

INTEGRATED AC TRANSMISSION NETWORK EXPANSION AND REACTIVE POWER PLANNING*

M. RAHMANI AND M. RASHIDINEJAD**

Dept of Electrical Engineering, Shahid Bahonar University of Kerman, Kerman, I. R. of Iran
Email: mrashidi@uk.ac.ir

Abstract– An integrated technique for solving transmission network expansion planning considering the allocation of reactive power sources using an AC model is presented in this paper. Embedding reactive power management in TNEP is a challenging task since AC load flow may not converge in absence of proper reactive power allocation. Usually transmission expansion planning and reactive power planning are considered as two distinct problems, but in this paper both problems are investigated concurrently. These two problems can be integrated because there is an inherent interaction between transmission line capacity and reactive power sources. In power systems, transferring reactive power may engage line capacity which requires more new transmission lines, while allocating reactive power sources close to the load centers may prevent the addition of new transmission lines. On the other hand, if reactive power sources are not included, real power losses will increase considerably and thereby reduce transmission line capacities. The main objective of this study is to show that both active and reactive power planning can be handled simultaneously. This non-convex combinatorial optimization problem is solved here using a real genetic algorithm (RGA). Significant results through case studies of two test systems show the advantages of the proposed integrated network planning.

Keywords– Transmission expansion planning, real genetic algorithm, reactive power planning, AC optimal power flow, VAR sources

1. INTRODUCTION

Transmission network expansion planning (TNEP) and reactive power planning (RPP) are crucial issues, especially in deregulated power systems. In the environment of a restructured electricity industry, open access to transmission systems introduces new challenges to market participants. As electricity consumption grows, new transmission lines are needed to provide alternative paths for power transfer from generators to load centers to assure continuous supply. On the other hand, reactive power sources are desired to support available transfer capability (ATC), power factor correction, loss reduction and voltage profile improvement. The voltage collapse phenomenon and other instability problems can be related to the system's inability to meet reactive power demands. When AC model is used for TNEP, it makes sense to consider reactive power allocation simultaneously, because lack of reactive power support can lead to either 1) no convergence of the load flow program or 2) unrealistic results due to Q absorption by generators due to line charging VARs or 3) unacceptably low voltages in the system [1].

Despite the implicit interdependence of RPP and TNEP, due to the complexity of merging these two problems, each problem is solved separately. In this study a new methodology is proposed to solve these complicated problems concurrently. In the traditional approach, transmission network planning problem is

*Received by the editors August 31, 2010; Accepted December 11, 2011.

**Corresponding author

solved using simplified models. The transportation model, the hybrid model, the linear disjunctive model, and the DC model [2], among others, are used in this first stage, and the problem is solved through classical optimization techniques [3–6] as well as evolutionary algorithms such as simulated annealing [7], genetic algorithms [8-10], tabu search [11], GRASP [12], ant colony [13] and also hybrid heuristic algorithms [14]. Then, in a subsequent stage, the obtained expansion network is reinforced with new lines and reactive power sources [15-20] to satisfy all requirements of a real AC network. The problem of dealing with real power losses, reactive power demands, incorporating FACTS devices into the system, voltage stability and other operational requirements are other issues that may arise when working with the DC model in transmission planning. Since active and reactive power planning are dependent on each other, these approaches may not achieve the optimal solution. The interdependence of transmission lines and reactive power sources can be addressed as follows:

1. Reactive power demands: these are an inherent part of any load center and must be procured either locally, through reactive sources, or produced by generators and transferred through transmission lines.
2. Real power losses: these also occur in any transmission network and reduce transmission capacity effectively. Transmission line capacity can be increased by line reinforcement or reactive power support.

In this study a comprehensive model for integrated transmission expansion and reactive power planning using the AC model is employed.

Integrated transmission expansion and reactive power planning is a very complex mixed integer nonlinear programming problem and becomes more complicated, especially when the size of the transmission network increases. The use of metaheuristic approaches seems to be necessary for solving such a non-convex problem. In this study a real genetic algorithm (RGA) [14, 21] is used to solve the planning problem, since GA is suitable for multi-objective optimization problems resulting in good solutions while maintaining low computational efforts. RGA is used to handle discrete variables in a major problem and a nonlinear constrained optimization for fitness function evaluation is solved in a minor problem. The objective function of the minor problem is minimum active power losses associated with the minimum value of reactive power sources.

This paper is organized as follows: section 2 gives an overview of the TNEP-RPP problem, section 3 presents mathematical modeling of combined AC TNEP-RPP; in section 4, the optimization process is described; in section 5, a modified Garver system is used as an illustrative example and for further analysis of the proposed method; in section 6, a modified IEEE 24-bus system is employed as another practical case study. Conclusions are made in section 7.

2. OVERVIEW OF TNEP-RPP PROBLEM

The main objective of the TNEP-RPP problem is to determine where, how many and when new devices (transmission lines and reactive power sources) must be added to the network in order to make its operation viable for a pre-defined horizon of planning, at a minimum cost. Currently, there is no technical literature on solving AC TNEP-RPP concurrently. The use of a complete AC model of the transmission network expansion planning problem is incipient, and there are few reports discussing the reactive power planning in TNEP problem. In [1] the authors firstly carried out the short term TNEP problem only in existing right-of-ways, and then reactive power allocation is implemented using a heuristics algorithm. In [21] the authors proposed a three step plan for solving the TNEP-RPP problem; in the first step the DC TNEP is solved, in the next step the AC TNEP, supplying the reactive power locally, is used for line reinforcement in order to deal with power losses, and in the third step, removing local reactive power

sources from step 2, the RPP problem is solved to find the location and minimum capacities of the VAR-plants needed for feasible system operation. In [22] a constructive heuristic algorithm (CHA) is proposed to allocate transmission lines in an iterative manner, while the reactive sources are allocated prior to lines allocation at weak buses using an index obtained by the Lagrange multiplier of the reactive power balances in each bus. The main characteristics of [1, 21-22] are that all of them solve the TNEP-RPP in several steps where it seems difficult to obtain the optimum solutions by these methods.

3. MATHEMATICAL MODELING

A mathematical model for the TNEP and RPP problem can be formulated in equations (1–11):

$$\min v_0 = \mathbf{c}^T \mathbf{n} \quad (1)$$

$$\min v_1 = K_e P_{Loss} D + F(\mathbf{q}, \mathbf{x}) \quad (2)$$

s.t.

$$\mathbf{P}(\mathbf{U}, \theta, \mathbf{n}) - \mathbf{P}_G + \mathbf{P}_D = \mathbf{0} \quad (3)$$

$$\mathbf{Q}(\mathbf{U}, \theta, \mathbf{n}) - \mathbf{Q}_G + \mathbf{Q}_D - \mathbf{q} = \mathbf{0} \quad (4)$$

$$\underline{\mathbf{P}}_G \leq \mathbf{P}_G \leq \overline{\mathbf{P}}_G \quad (5)$$

$$\underline{\mathbf{Q}}_G \leq \mathbf{Q}_G \leq \overline{\mathbf{Q}}_G \quad (6)$$

$$\underline{\mathbf{q}} \leq \mathbf{q} \leq \overline{\mathbf{q}} \quad (7)$$

$$\underline{\mathbf{U}} \leq \mathbf{U} \leq \overline{\mathbf{U}} \quad (8)$$

$$(\mathbf{N} + \mathbf{N}^0) \mathbf{S}^{\text{from}} \leq (\mathbf{N} + \mathbf{N}^0) \overline{\mathbf{S}} \quad (9)$$

$$(\mathbf{N} + \mathbf{N}^0) \mathbf{S}^{\text{to}} \leq (\mathbf{N} + \mathbf{N}^0) \overline{\mathbf{S}} \quad (10)$$

$$0 \leq \mathbf{n} \leq \overline{\mathbf{n}} \quad (11)$$

n and u are integer and θ is unbounded

where: \mathbf{c} and \mathbf{n} represent the costs vector of the prospective transmission lines and the prospective transmission lines, respectively. \mathbf{N} and \mathbf{N}^0 are diagonal matrices containing prospective and the existing circuits, respectively. K_e is the cost of energy, D is the system operating time, P_{Loss} is the total real power loss, $F(\mathbf{q}, \mathbf{x})$ is the cost function of VAR sources and \mathbf{q} is the MVAR size of the VAR sources vector. \mathbf{x} is the binary vector that indicates whether or not to install reactive power sources at load buses. v_0 is the investment due to the addition of new circuits to the networks; v_1 is the total cost of active power losses and VAR sources. $\overline{\mathbf{n}}$ is the vector containing the maximum number of prospective transmission lines. θ is the phase angle vector. \mathbf{P}_G and \mathbf{Q}_G are the existing real and reactive power generation vectors. \mathbf{P}_D and \mathbf{Q}_D are the real and reactive power demand vectors; \mathbf{U} is the voltage magnitude vector; $\overline{\mathbf{P}}_G$, $\overline{\mathbf{Q}}_G$ and $\overline{\mathbf{U}}$ are the vectors of the maximum limits of generation of real power, reactive power and voltage magnitudes, respectively; $\underline{\mathbf{P}}_G$, $\underline{\mathbf{Q}}_G$ and $\underline{\mathbf{U}}$ are the vectors of the minimum limits of generation of real power, reactive power and voltage magnitudes, respectively. In this study 105% and 95% of the nominal value are used for the maximum and minimum voltage magnitude limits, respectively. \mathbf{S}^{from} , \mathbf{S}^{to} and $\overline{\mathbf{S}}$

are the apparent power flow vectors (MVA) in the branches in both terminals and their limits. The objective function Eq. (1) considers only the expansion costs of transmission lines, while the objective function Eq. (2) considers the minimum cost of power losses associated with the costs of VAR sources that can be installed. Equations (3) and (4) represent the conventional equations of AC power flow considering \mathbf{n} , the number of circuits (lines and transformers), and \mathbf{q} , the size of VAR sources, as variables. The limits for real and reactive power in the generators are represented by Eq. (5) and Eq. (6), respectively; for VAR sources by Eq. (7) and for the voltage magnitudes by Eq. (8). The limits (MVA) of the flows are represented by Eq. (9) and Eq. (10). The constraints in the capacities of the added circuits are represented by Eq.(11). The costs of the VAR sources can be defined as follows:

$$F(\mathbf{q}, \mathbf{x}) = \sum_{k \in \Omega_l} (c_{0k} + c_{1k} q_k) x_k \quad (12)$$

where Ω_l represents the set of all load buses, and c_{0k} and c_{1k} are the installation cost and unit cost of the VAR source at bus k . q_k is the MVAR size of VAR source at bus k . x_k is a binary variable that indicates whether or not to install reactive power source at bus k . The active power losses can be calculated by the following equation:

$$P_{Loss} = \sum_{ij \in \Omega} [U_i^2 + U_j^2 - 2U_i U_j \cos(\theta_i - \theta_j)] g_{ij} \quad (13)$$

Where: Ω is the set of all transmission lines, U_i and θ_i are the magnitude and angle of voltage at bus i . g_{ij} is the conductance of the line between buses i and j . The $\mathbf{P}(\mathbf{U}, \theta, \mathbf{n})$ and $\mathbf{Q}(\mathbf{U}, \theta, \mathbf{n})$ in equations (3) and (4) are basic AC power flow elements and they are given various papers [21-23]. The integer variable \mathbf{n} , the number of circuits added in branch ij , and the binary variable \mathbf{x} , and connection or disconnection of VAR sources to a load bus are the most important decision variables, and a feasible operation solution of the electric power system depends on these values. The remaining variables only represent the operating state of a feasible solution. For a feasible investment proposal, defined through specified values of \mathbf{n} and \mathbf{x} , one can have several feasible operation states.

4. OPTIMIZATION PROCESS

In this paper a real genetic algorithm (RGA) [14, 21] is employed to solve the planning problem. Mathematically, GA can be considered a technique for the optimization of combinatorial large and complex problems with a high probability of finding the global optimum among many local optimal solutions [24]. The RGA has the following special characteristics: 1) it does not require any binary coding or decoding stages; 2) it is faster and more accurate than binary GA. In this study RGA is used to identify the most attractive lines and reactive power (VAR) sources for installation. To this end, each combination of new lines and reactive power sources, the so-called individuals, are embedded into the initial network, and an AC-OPF is consequently solved. The objective function of AC-OPF is minimum costs of active power losses as well as minimum costs of VAR sources. The total costs of new lines in association with the costs of VAR sources and the amount of satisfaction of constraints are used to evaluate the fitness of each individual. Once we have the genetic representation and the fitness function defined, GA proceeds to initialize a population of solutions randomly, and then improve it through repetitive application of selection, recombination, and mutation operators. The overall procedure of implementing RGA in TNEP considering reactive power allocation is shown in Fig. 1.

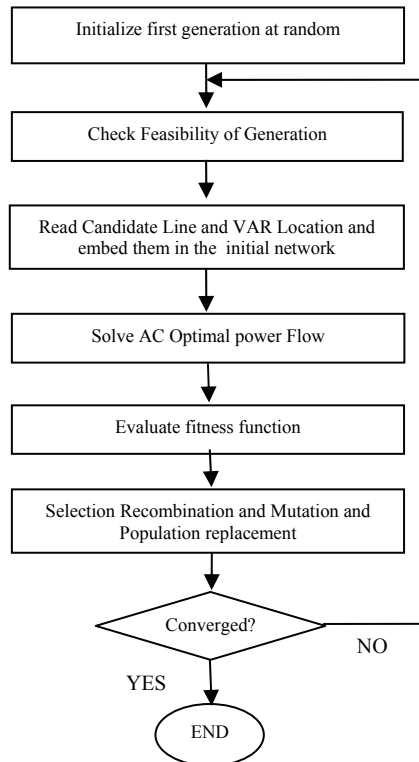


Fig. 1. Flowchart of the TNEP considering reactive power allocation using RGA

Different steps to find the optimum solution for TNEP-RPP are described as follows:

a) Initialization of the first generation

Each individual is chosen in a random fashion, while the data of an individual are the number and location of new lines as well as the location of VAR sources at load buses. The individual is a solution proposal for the planning problem, or better yet, is the topology made up of all transmission lines and reactive power sources added to the system corresponding to an investment proposal. In TNEP-RPP individuals are represented by a vector size. Each vector is constructed as the number of new transmission lines that are proposed to be added to respective branches and those load buses that VAR sources might be allocated to [25]. The value of each new transmission line can vary between zero and the maximum number of lines. For reactive power sources, two choices are possible: whether to install reactive power sources or not. Thus in the codification shown in Fig. 2, branch 2–6 has two new lines; branch 3–5 has one new line and bus 4 is a candidate for reactive power sources.

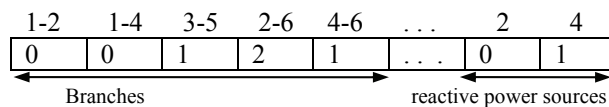


Fig. 2. Codification proposal

b) Feasibility checking

In TNEP-RPP, which is NP-hard [1], computational requirements of an optimization solver blow out with the dimensionality of the problem. Hence, the solution of TEP problem within the framework of optimization generally requires a reduction in search space. In order to reduce the search space of the problem each individual is checked in terms of costs; those individuals whose investments are too high will be pruned

out. However, it should be noted that setting a low threshold for pruning individuals may cause the algorithm to lose the optimum solution or even the high quality solutions.

c) *Setting up the network*

Read out the data of each individual, consisting of the number and location of new lines and the location of VAR sources and construct the new network. However, some individuals may create an unconnected network. The unconnected network may consist of several subsystems. A subsystem is referred to as a set of buses and transmission lines which are not connected to other subsystems. In this case special care should be taken into account when solving the AC optimal power flow. A common task for this difficulty is to solve an AC-OPF for each subsystem, and then sum up the objective function of each AC-OPF as the overall objective function.

d) *Solving AC-OPF*

For each individual, solve a particular AC optimal power flow with real and reactive power sources as optimization objectives. In this step the following problem is solved:

$$\min v_1 = K_e P_{\text{Loss}} D + f(\mathbf{q}) \quad (14)$$

st.

$$\mathbf{P}(\mathbf{U}, \theta) - \mathbf{P}_G + \mathbf{P}_D = 0 \quad (15)$$

$$\mathbf{Q}(\mathbf{U}, \theta) - \mathbf{Q}_G + \mathbf{Q}_D - \mathbf{q} = \mathbf{0} \quad (16)$$

$$\underline{\mathbf{P}}_G \leq \mathbf{P}_G \leq \overline{\mathbf{P}}_G \quad (17)$$

$$\underline{\mathbf{Q}}_G \leq \mathbf{Q}_G \leq \overline{\mathbf{Q}}_G \quad (18)$$

$$\underline{\mathbf{q}} \leq \mathbf{q} \leq \overline{\mathbf{q}} \quad (19)$$

$$\underline{\mathbf{U}} \leq \mathbf{U} \leq \overline{\mathbf{U}} \quad (20)$$

$$\mathbf{S}^{\text{from}} \leq \overline{\mathbf{S}} \quad (21)$$

$$\mathbf{S}^{\text{to}} \leq \overline{\mathbf{S}} \quad (22)$$

θ is unbounded.

When new lines are embedded in the initial network, there is no need to separate the existing lines from new lines; i.e. all lines are existing lines. Also, since new VAR sources are included in the system, the binary variable vector \mathbf{x} , connection or disconnection of a VAR source to a load bus is unnecessary in this formulation. There is no integer variable in this formulation, so we just need to solve an AC OPF. This problem can be solved using any nonlinear programming software.

e) *Fitness function evaluation*

The fitness function is required by genetic algorithm in order to evaluate the quality of the individual of a population. This paper uses the fitness function proposed in [14, 21], however, for a quick reference it is also provided in this subsection. The fitness function of the RGA method in this paper attempts to minimize three objectives: a) deviation from OPF constraint limits; b) costs of installation for the new transmission lines; c) costs of allocation of VAR sources. To calculate the fitness value, a fuzzy numbers technique is adopted in this research. The choice of fuzzy numbers is due to the linguistic and qualitative

behavior of the aforementioned objectives. However, other techniques could be implemented to calculate fitness. The fitness of a solution is assessed against the degree of membership of a specific solution to a given membership function [26, 27], where higher membership values imply a better solution, as described in Fig. 3.

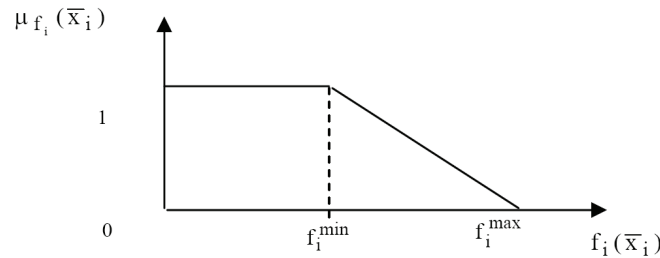


Fig. 3. A typical membership function

Membership values can be represented by Eq. (23) which lies between 0 and 1, where $h_i(f(\bar{X}))$ is a strictly monotonically decreasing function that can be either linear or nonlinear.

$$\mu_{f_i}(\bar{X}) = \begin{cases} 1 & \text{if } f_i(\bar{X}) < f_i^{\min} \\ h_i(f(\bar{X})) & \text{if } f_i^{\min} \leq f_i(\bar{X}) \leq f_i^{\max} \\ 0 & \text{if } f_i(\bar{X}) > f_i^{\max} \end{cases} \quad (23)$$

Since the main objective of a TNEP-RPP is to minimize the costs of new transmission lines and VAR sources such that all constraints must be satisfied, fitness evaluation can be based upon Eq. (24).

$$fitness = w_1\mu_1(v_0) + w_2\mu_2(v_1) + w_3(\mu_3(d_V) + \mu_4(d_G) + \mu_5(d_S)) \quad (24)$$

Where all terms of the fitness function are fuzzy numbers with the appropriate membership function. w_1 , w_2 and w_3 are tuning weights which can be selected by a decision satisfying Eq. (25).

$$w_1 + w_2 + w_3 = 1 \quad (25)$$

v_0 is the total cost of new lines and v_1 is the total cost of VAR sources. d_V , d_G and d_S are the sum of constraints deviations from voltage limits, power generation limits and branch flow limits, respectively. These Parameters are obtained after solving the AC OPF discussed in the last subsection. The range of fitness function is between 0 and 1, such that when the fitness value equals one it means that the costs of new transmission lines as well as the costs of VAR plants are zero ($v_0 = 0$, $v_1 = 0$). It can also be said that the deviations from the AC OPF constraints are zero, which means that all decision variables are inside their limits ($d_V = 0$; $d_G = 0$; $d_S = 0$).

f) Real genetic operators

When OPF is solved for the entire individuals and the fitness values of each is figured out, the selection, recombination, and mutation operators of RGA are implemented in order to construct a new generation of individuals. These operators are not described in this paper. A detailed discussion about RGA operators is given in [14, 21, 23].

5. CASE STUDIES

The algorithm is implemented in MATLAB platform using a 3 GHZ dual core CPU with 3 GB memory RAM. The Garver systems [2] and the IEEE 24-bus RTS [28] are used as case studies in this paper.

Unfortunately, we were unable to compare the results of this paper with other papers since the TNEP problem and RPP are usually solved and reported separately. There are only a few works that consider both TNEP and RPP jointly. However, the case studies proposed in [1], [21- 23] were found insufficient for implementing in this paper. In [1] the case studies and the proposed strategy, the possibility of installing the new transmission lines in the system is not considered; it only considers the reinforcement of the existing transmission lines. In [21- 23] the authors modified the original data provided in [1, 29] in which the generators and maximum flow capacity of transmission lines are augmented; modifying the tests systems will not provide the planner with the importance of implementing of TNEP-RPP and the necessary reinforcement of the system when compared with DC TNEP reported in many papers. To implement RGA for optimum TNEP-RPP, a population of 100 individuals is used, while recombination and mutation rates are 76 % and 3 %, respectively. The selection process would be terminated when there is no new individual in the population. Since in GA new generation may consist of previous individuals, a pool of all individuals is constructed to speed up the process. To calculate the fitness function for repetitive individuals we do not carry out all the calculations and simply pull out the fitness values from the pool. All calculations are carried out for the new individuals and, finally, their data and fitness values are inserted into the pool. One of the important parameters in this paper is the cost of energy K_e . This parameter depends on the average cost of energy in a year. For example, the values for peak wholesale and average retail electricity prices in the United States for the year 2006 are given in [29]. However, the updated prices can be obtained from [30]. This paper does not obtain the updated cost of energy since the costs of transmission lines are not updated. Instead these parameters are adjusted in a manner to be comparable with the transmission lines cost. In this paper, since the cost of energy is provided annually, the cost of transmission lines must also be provided annually. It is usually assumed that a line built today will be operative for several years [31]. To have an estimate of the annual transmission line costs the capital recovery factor might be calculated as $(1+i)^n / [(1+i)^n - 1]$, where i is the discount rate and n is the number of years [31]. This paper assumes that the provided costs of energy for case studies in [2, 28] are annual.

a) Garver 6-bus system

For the illustrative examples, the Garver 6-bus system is used. This system has 6 buses and 15 branch candidates with a total demand of 760 MW and 190 MVar, and a maximum of 5 lines can be added to each branch. Since the real transmission lines have shunt susceptances that represent significant sources of reactive power, the Garver system is modified to contain shunt susceptances. In this case, $b_{ij} = .03X_{ij}$ was added for each transmission line. The modified Garver system data is provided in Appendix A.

- TNEP-RPP for the Garver System

To locate transmission lines and allocate reactive power sources, 10 independent runs of the RGA with different random seeds are conducted. Each run of RGA converges after approximately 6 generations and solves about 175 OPF, and about 70% of the runs get optimal solutions. In this example, the fixed costs of VAr installation is $c_0 = 0.1 \text{ UM}$ (UM: Monetary Unit) and the VAr variable cost is $c_1 = 0.3 \text{ UM} / \text{MVar}$, while $K_e D$ is set to 1 (see equations (2) and (12)).

RGA finds the two following solutions for the Garver system:

1. In the first solution, as shown in Fig. 4, the line costs are UM 250.000 with the following details: $n_{2-6} = 4$, $n_{3-5} = 2$; $n_{4-6} = 3$. Also, a total of 68.5 MVar reactive sources should be installed at buses 2 and 5. Active and reactive power losses are 55.00 MW and 210.38 MVar, respectively.

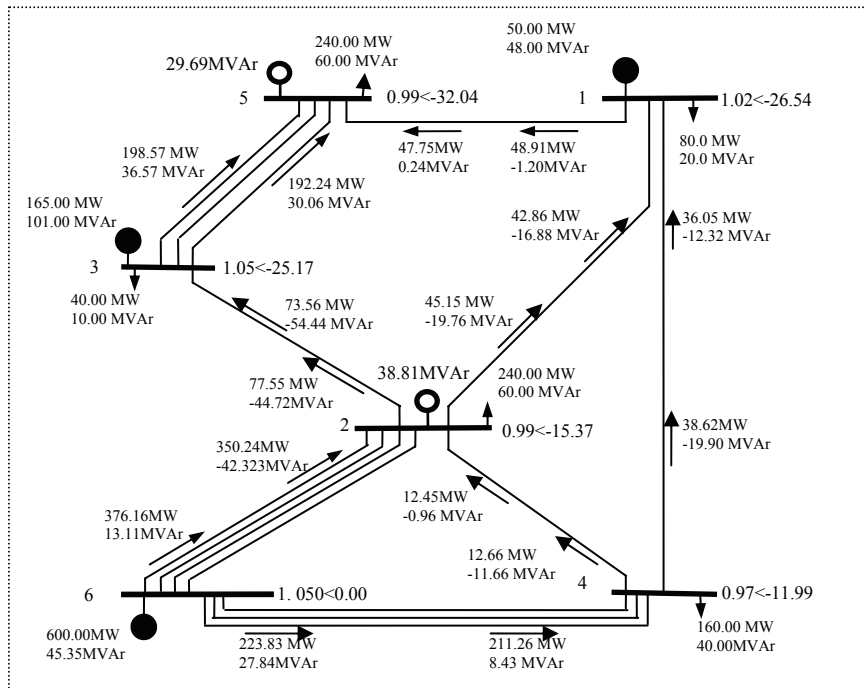


Fig. 4. Simultaneous planning for modified Garver system solution 1

The line costs for the second solution are UM 250.000 with a different topology, $n_{2-6} = 5$; $n_{3-5} = 2$; $n_{4-6} = 2$ and a total of 57.6 MVar is needed for installation at buses 4 and 5. Active and reactive power losses are 55.00 MW and 210.40 MVar, respectively. Figure 5 shows the complete results for this solution. Detailed investment for transmission lines, VAr sources and real power losses are given in Table 1.

Table 1 Results for the Garver System

Costs (US \$)	Garver system (Solution 1)	Garver system (Solution 2)
Transmission lines	250.000 ($n_{2-6} = 4; n_{3-5} = 2; n_{4-6} = 3$)	250.000 ($n_{2-6} = 5; n_{3-5} = 2; n_{4-6} = 2$)
Power losses	55.000	55.000
VAr sources	20.750	17.480
Total	325.750	322.480

As indicated, with different topologies, transmission line costs are equal for both solutions, but solution 2 is preferred since it has a lower total investment cost. The results obtained through this example illustrate a significant realization of simultaneous transmission expansion and reactive power source allocation. Additionally, the final topology may have a reliable operation when tested with an AC power flow, so the solution may not require additional transmission line reinforcement. Such reinforcements, starting with the transmission line planning, are generally necessary when a DC model is used to handle the planning process. The solution for a DC model of this system is reported in [2, 9], where the investment cost is UM 200.000 with installation of the following lines: $n_{2-6} = 4$; $n_{3-5} = 1$; $n_{4-6} = 2$. This solution falls short when AC network is considered, however, the results obtained in this section provide the planner with the exact topology in the real system conditions (AC Network).

b) IEEE-24 bus system

The IEEE 24-bus system data is given in [28] and depicted in Fig. 6. This system is to expand to a future condition with generation levels and the loads three times their original values (i.e, up to a total

10215 Mw maximum generation capacity and 8550 Mw peak demand). Therefore there appears to be enough generation capacity, but according to [28], it is shown that new lines are required to be installed to avoid load curtailment. The IEEE 24-bus system has 24 buses and 41 transmission lines. In this case the VAr fixed cost of installation is considered to be $c_0 = 10000$ US\$ and the VAr variable cost is $c_1 = 3$ US\$/kVAr. The cost of energy (k_e) is considered to be 0.06 \$/KWhour and system duration time is $D = 1 * 365 * 24$ (hour) for a one-year planning horizon.

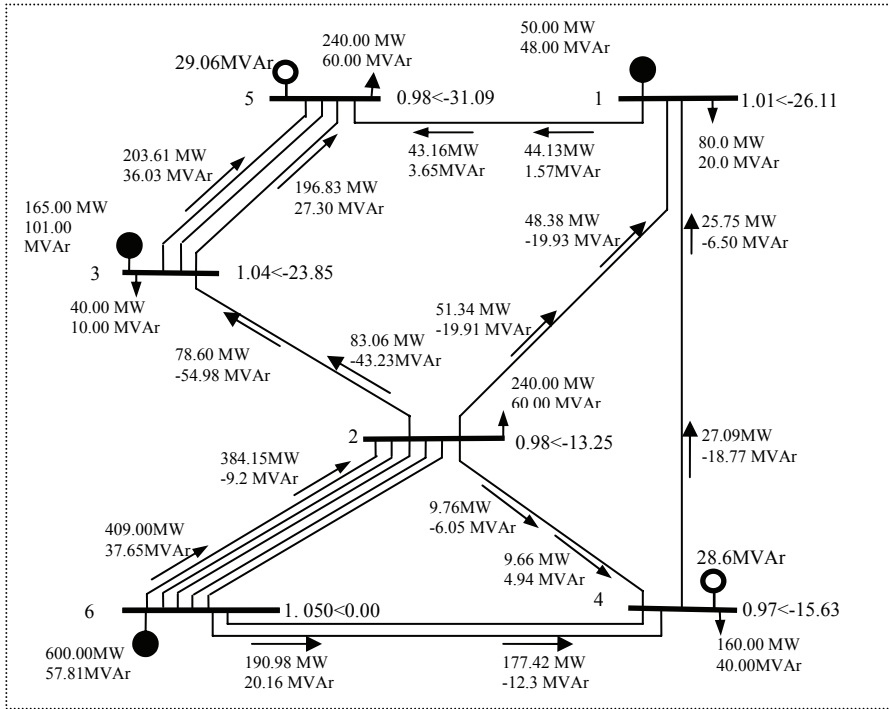


Fig. 5. Simultaneous planning for modified Garver system solution 2

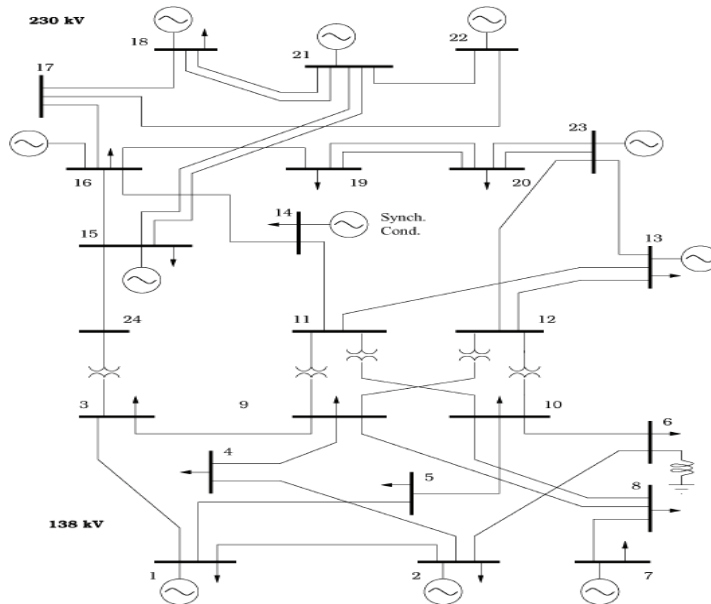


Fig. 6. IEEE 24-bus System [28]

RGA is used to find the optimal solution for the TNEP-RPP in a unique stage, while twenty independent runs of RGA are implemented to find a solution. Each run of RGA converges after an average of 15 generations, solving about 210 OPF. About 40% of the runs have optimal solutions. Results are obtained

by the following new lines: $n_{7-8} = 2$; $n_{6-10} = 2$; $n_{14-16} = 1$; $n_{10-12} = 1$. A total of 901.48 MVar reactive sources are installed at buses 3, 8, 9, 11 and 12, with the size of 170.34, 109.14, 210.15, 172.61 and 239.23 MVar, respectively. Active and reactive power losses are 209.15 MW and 780 MVar, respectively. The total investment is US\$ 280,684,410, which is shown in Table 2.

Table 2. Overall results for the IEEE 24-bus system

Costs (US \$)	IEEE 24 Bus System
Transmission Lines	168,000,000 ($n_{7-8} = 2; n_{6-10} = 2; n_{14-16} = 1; n_{10-12} = 1$)
Power Losses	109,930,000
VAr sources	2,754,410
Total	280,684,410

The optimum solution for DC model is reported in [9], with 152,000,000 investment on the following transmission lines: $n_{7-8} = 2$; $n_{6-10} = 1$; $n_{14-16} = 1$; $n_{10-12} = 1$. However, this topology is not able to provide a viable operation when considering the complete AC network where power losses and reactive demands play an important role in the network. The solution provided for the AC model of the IEEE-24 bus system in this paper shows the importance of integrated transmission and reactive power planning. The result of the AC OPF with the proposed transmission lines and reactive sources is given in Tables 3 and 4. Table 3 shows the results related to the system buses, while Table 4 shows branch results. The voltage magnitude and angle, the real and reactive power demand, the real and reactive power generation and the allocated reactive power sources at system buses are shown in Table 3. The results related to the system branches in Table 4 contain: the existing and new transmission lines, the active, reactive and apparent power flow at each end of the transmission lines and the active and reactive power losses.

Table 3. Detailed results of the IEEE 24-buses system (Bus View) [28]

Bus	Type	Vm (Volt)	Teta (Rad)	P _D [MW]	Q _D [MVar]	P _G [MW]	Q _G [MW]	VAR [MVar]
1	V0	1.03	0	324	66	569.33	-79.46	0
2	PV	1.05	-0.03	291	60	576	219.57	0
3	PQ	0.96	-11.12	540	111	0	0	170.34
4	PQ	0.96	-11	222	45	0	0	0
5	PQ	0.99	-8.16	213	42	0	0	0
6	PV	1.04	-10.07	408	84	0	-262.11	0
7	PV	1.05	-1.33	375	75	899.19	104.11	0
8	PQ	1.02	-6.98	513	105	0	0	109.14
9	PQ	1.01	-7.32	525	108	0	0	210.15
10	PQ	1.05	-6.65	585	120	0	0	0
11	PQ	1.04	8.17	0	0	0	0	172.61
12	PQ	1.02	7.64	0	0	0	0	239.23
13	PV	1.05	20.23	795	162	1489.42	274.21	0
14	PV	1.05	12.58	582	117	0	331.91	0
15	PV	1.03	22.01	951	192	645	330	0
16	PV	1.04	20.91	300	60	465	240	0
17	PQ	1.04	27.78	0	0	0	0	0
18	PV	1.05	31.11	999	204	1180.91	232.95	0
19	PQ	1.01	21.57	543	111	0	0	0
20	PQ	1.02	28	384	78	0	0	0
21	PV	1.05	32.89	0	0	1149.40	5.19	0
22	PV	1.05	31.17	0	0	13.53	-13.50	0
23	PV	1.05	33.53	0	0	1771.38	236.59	0
24	PQ	0.95	10.14	0	0	0	0	0
Total				8550	1740	8759.15	1619.45	901.48

Table 4. Detailed result of the IEEE 24-buses system (Branch View) [28]

from	to	N_{ij}	N_{ij}^0	P_{ij} [MW]	Q_{ij} [MW]	S_{ij} [MW]	P_{ji} [MW]	Q_{ji} [MW]	S_{ji} [MW]	Loss P [MW]	Loss Q [MW]	S_{ij}^{max} [MW]
1	2	0	1	-24.34	-173.30	175	24.90	126.44	128.87	0.56	-46.86	175
1	3	0	1	94.99	17.23	96.54	-90.13	-4.06	90.22	4.86	13.17	175
1	5	0	1	174.68	10.61	175	-168.37	11.50	168.76	6.31	22.11	175
2	4	0	1	163.71	46.42	170.16	-155.04	-16.40	155.91	8.67	30.02	175
2	6	0	1	96.39	-13.29	97.30	-92.15	23.98	95.22	4.24	10.69	175
3	9	0	1	-60.19	-26.85	65.90	61.63	29.30	68.24	1.44	2.46	175
3	24	0	1	-389.69	90.25	400	393.72	56.87	397.80	4.03	147.11	400
4	9	0	1	-66.96	-28.60	72.81	68.48	31.79	75.50	1.53	3.19	175
5	10	0	1	-44.63	-53.50	69.67	45.72	55.25	71.71	1.09	1.74	175
6	10	2	1	-315.85	-370.09	486.55	320.16	-416.08	525	4.31	-786.17	525
7	8	2	1	524.19	29.11	525	-510.93	16.74	511.21	13.26	45.85	525
8	9	0	1	5.55	4.79	7.33	-5.52	-9.27	10.79	0.03	-4.48	175
8	10	0	1	-7.62	-17.39	18.98	7.73	13.04	15.16	0.12	-4.35	175
9	11	0	1	-332.71	18.52	333.22	335.22	73.08	343.09	2.51	91.60	400
9	12	0	1	-316.89	31.82	318.48	319.18	51.86	323.37	2.29	83.68	400
10	11	0	1	-330.41	66.58	337.05	332.78	19.91	333.37	2.37	86.49	400
10	12	1	1	-628.21	161.22	648.57	632.60	-1.10	632.60	4.39	160.12	800
11	13	0	1	-467.67	79.68	474.41	480.46	9.18	480.54	12.78	88.86	500
11	14	0	1	-200.32	-0.06	200.32	202.33	6.04	202.42	2.01	5.98	500
12	13	0	1	-484.34	55.04	487.46	498.20	42.36	500	13.86	97.41	500
12	23	0	1	-467.44	133.43	486.11	495.73	65.17	500	28.30	198.60	500
13	23	0	1	-284.24	60.66	290.64	292.87	-13.40	293.18	8.64	47.26	500
14	16	1	1	-784.33	208.87	811.67	799.36	-109.82	806.87	15.03	99.05	1000
15	16	0	1	108.51	-80.83	135.31	-108.14	79.88	134.44	0.37	-0.94	500
15	21	0	2	-819.94	81.95	824.03	840.23	53.63	841.94	20.29	135.58	1000
15	24	0	1	405.43	136.87	427.91	-393.72	-56.87	397.80	11.71	80.01	500
16	17	0	1	-492.17	69.80	497.09	499.73	-16.36	500	7.56	53.44	500
16	19	0	1	-34.05	140.13	144.21	34.65	-140.61	144.82	0.60	-0.48	500
17	18	0	1	-438.70	24.46	439.38	441.89	-2.28	441.90	3.19	22.18	500
17	22	0	1	-61.03	-8.10	61.57	61.49	-12.54	62.76	0.46	-20.64	500
18	21	0	2	-259.98	31.23	261.85	261.01	-35.15	263.37	1.03	-3.92	1000
19	20	0	2	-577.65	29.61	578.41	586.05	18.44	586.34	8.40	48.05	1000
20	23	0	2	-970.05	-96.44	974.83	982.77	184.82	1000	12.72	88.37	1000
21	22	0	1	48.15	-13.29	49.95	-47.96	-0.96	47.97	0.19	-14.26	500
Total		6								209.15	780.92	

6. CONCLUSION

In this paper, a mathematical model and a metaheuristic technique for solving the integrated transmission expansion and reactive power planning problems using AC model are presented. The main contribution of this paper is to show that active and reactive power planning can be carried out simultaneously. A real genetic algorithm is employed to solve this kind of multi-objective optimization problem. The fitness function is derived from the investments in new lines associated with the costs of VAR sources, as well as AC optimal power flow constraints violation. AC optimal power flow tries to minimize the costs of real power losses as well as the investment in VAR sources. An illustrative example on the modified Garver system associated with a general analysis of the results is discussed. The IEEE 24-bus system is used as a practical case study, and the simulation results show a significant performance of the proposed methodology.

REFERENCES

1. Gajbhiye, R. K., Naik, D., Dambhare, S. & Soman, S. A. (2008). An expert system approach for multi-year short-term transmission system expansion planning: An Indian experience. *Power Systems, IEEE Transactions on*, Vol. 23, No. 1, pp. 226-237.
2. Romero, R., Monticelli, A., Garcia, A. & Haffner, S. (2002). Test systems and mathematical models for transmission network expansion planning. *IEE Proc. Gen. Trans. Distrib.*, Vol. 149, No. 1, pp. 27-36.
3. Romero, R. & Monticelli, A. (1994). A hierarchical decomposition approach for transmission network expansion planning. *IEEE Trans. Power Syst.*, Vol. 9, No. 1, pp. 373-380.
4. Rider, M. J., Garcia, A. V. & Romero, R. (2008). Transmission system expansion planning by a branch-and-bound algorithm. *IET Gener. Trans. Distrib.*, Vol. 2, No. 1, pp. 90-99.
5. Binato, S, Pereira, M. V. F. & Granville, S. (2001). A new Benders decomposition approach to solve power transmission network design problems. *IEEE Trans. Power Syst.*, Vol. 16, No. 2, pp. 235-240.
6. Alguacil, N., Motto, A. L. & Conejo, A. J. (2003). Transmission expansion planning: a mixed-integer LP approach. *IEEE Trans. Power Syst.*, Vol. 18, No. 3, pp. 1070-1077.
7. Gallego, R. A., Alves, A. B., Monticelli, A. & Romero, R. (1997). Parallel simulated annealing applied to long term transmission network expansion planning, *IEEE Trans. Power Syst.*, Vol. 12, No. 1, pp. 181-188.
8. Gallego, R. A, Monticelli, A. & Romero, R. (1998). Transmission systems expansion planning by an extended genetic algorithms. *IEE Proc. Gen. Trans. Distrib.*, Vol. 145, No. 3, pp. 329-335
9. Romero, R., Rider, M. J. & Silva, I. D. J. (2007). A metaheuristic to solve the transmission expansion planning. *IEEE Trans. Power Syst.*, Vol. 22, No. 4, pp. 2289-2291.
10. Pavluchenko, D. A. & Manusov, V. Z. (2006). Electrical network optimization by genetic algorithm. *Euro. Trans. Electr. Power*; Vol. 16, pp. 569-576 .DOI: 10.1002/etep.104
11. Da Silva, E. L., Ortiz, J. M. A., De Oliveira, G. C. & Binato, S. (2001). Transmission network expansion planning under a Tabu search approach. *IEEE Trans. Power Syst.*, Vol. 16, No. 1, pp. 62-68.
12. Binato, S., De Oliveira, G. C. & De Araujo, J. L. (2001). A greedy randomized adaptive search procedure for transmission expansion planning. *IEEE Trans. Power Syst.*, Vol. 16, No. 2, pp. 247-253.
13. Paulun, T. (2006). Strategic expansion planning for electrical networks considering uncertainties. *Euro. Trans. Electr. Power*, Vol. 16, pp. 661-671.
14. Forghani, M. A., Seyed-Esfahani, M., Rashidinejad, M. & Farahmand, H. (2008). A goal attainment model for transmission expansion planning using a meta heuristic technique. *Iranian Journal of Science & Technology, Transaction B, Engineering*, Vol. 32, No. B3, pp. 235-247.
15. Wenjuan, Z., Fangxing, L. I. & Tolbert, L. M. (2007). Review of reactive power planning: objectives, constraints, and algorithms. *Power Systems, IEEE Transactions*, Vol. 22, No. 4, pp. 2177-2186.
16. Delfanti, M., Granelli, G., Marannino, P. & Montagna, M. (2000). Optimal capacitor placement using deterministic and genetic algorithms. *IEEE Trans. Power Syst.*, Vol. 15, No. 3, pp. 1041-1046.
17. Eghbal, M., Yorino, N., El-Araby, E. E. & Zoka, Y. (2008). Multi-load level reactive power planning considering slow and fast VAR devices by means of particle swarm optimisation. *Generation, Transmission & Distribution, IET*, Vol. 2, No. 5, pp.743-751.
18. Zhang, W. & Liu, Y. (2002). Optimal VAR planning in area power system. *Proc. Int. Conf. Power System Technology*, pp. 2072-2075.
19. Estevam, C. R. N., Rider, M. J, Amorim, E. & Mantovani, J. R. S. (2010). Reactive power dispatch and planning using a non-linear branch-and-bound algorithm. *Generation, Transmission & Distribution, IET*, Vol. 4, No. 8, pp.963-973.
20. Gallego, R. A., Monticelli, A. & Romero, R. (2001). Optimal capacitor placement in radial distribution networks. *IEEE Trans. Power Syst.*, Vol. 16, No. 4, pp. 630-637.

21. Rahmani, M., Rshidienjad, M. & Romero, R. (2010). Efficient method for AC transmission network expansion planning. *Electric Power Systems Research*, Vol. 80, No. 9, pp. 1056-1064.
22. Rider, M. J., Garcia, A. V. & Romero, R. (2007). Power system transmission network expansion planning using AC model. *IET Gener. Transm. Distrib.*, 2007, 1 (5), pp. 731–742.
23. Rahmani, M., Rashidinejad, M., Carreno, E. M. & Romero, R. A. (2010). A combinatorial approach for transmission expansion & reactive power planning. *Transmission and Distribution Conference and Exposition: Latin America (T&D-LA), 2010 IEEE/PES*, pp.529-536.
24. Goldberg, D. E. (1989). *Genetics algorithms in search, optimization and machine learning*. Addison–Wesley.
25. Niknam, T., Ranjbar, A. M., Shirani, A. R. & Ostadi, A. (2005). A new approach based on ANT algorithm for volt/var control in distribution network considering distribution generation. *Iranian Journal of Science & Technology, Transaction B, Engineering*, Vol. 29, No. B4.
26. Li-Xin, W. (1997). *A course in fuzzy systems and control*. Prentice Hall.
27. Choi, J, El-Keib. A. A. & Tran, T. (2005). A fuzzy branch and bound-based transmission system expansion planning for the highest satisfaction level of the decision maker. *IEEE Trans. Power Syst.*, Vol. 20, No. 1, pp. 475-484.
28. Fang, R. & Hill, D. J. (2003). A new strategy for transmission expansion in competitive electricity markets. *IEEE Trans. on Power Systems*, Vol. 18, No. 1, pp. 374–380.
29. Poonpun, P. & Jewell, W. T. (2008). Analysis of the cost per kilowatt hour to store electricity. *Energy Conversion, IEEE Transactions on*, Vol. 23, No. 2, pp.529-534.
30. <http://www.eia.gov/electricity/wholesale/index.cfm>
31. De la Torre, S., Conejo, A. J. & Contreras, J. (2008). Transmission expansion planning in electricity markets. *IEEE Trans. Power Syst.*, Vol. 23, No. 1, pp. 238–248.