IMPLEMENTATION OF SENSORLESS SPEED CONTROL FOR TWO-PHASE INDUCTION MOTOR DRIVE USING ISFOC STRATEGY

H. BEN AZZA1** M. JEMLI1, M. BOUSSAK2 AND M. GOSSA1

1 Unité de recherche en commande, surveillance et sûreté de fonctionnement des systèmes (C3S)
Equipe Développement des Systèmes Electrotechniques (DES)
Ecole Supérieure des Sciences et Techniques de Tunis (ESSTT)
5 Avenue Taha Hussein –BP 56, Bab Mnara 1008 Tunis – Tunisie
Email: benzzahechmi@voila.fr

2 Laboratoire des Sciences de l’Information et des Systèmes (LSIS) – UMR CNRS 6168
Centrale Marseille Recherche et Technologies (CMRT)
Ecole Centrale Marseille (ECM) – Technopôle Château Gombert –13451 – Marseille Cedex 20 – France

Abstract— This paper presents a new technique based on model reference adaptive system (MRAS) observer for sensorless speed control of Two-Phase Induction Motor (TPIM). The MRAS identification is performed by means of comparison of stator fluxes obtained from both stator and rotor equations with stator voltage and current measurements. Simulation and experimental results for a 1.1 kW TPIM set-up are presented and analysed using a dSpace system with a DS1104 controller board based on digital signal processor (DSP) TMS320F240. Simulation and experimental results at nominal, low and zero speeds confirm the effectiveness of the proposed sensorless speed controlled TPIM drive.

Keywords— Two-phase induction motor (TPIM), indirect stator-field-oriented control (ISFOC), model reference adaptive system (MRAS)

1. INTRODUCTION

Two-Phase Induction Motor (TPIM) is widely used in several industrial and domestic applications. In those applications the motor runs at constant frequency and is fed directly from the ac grid without any type of control strategy. The TPIM is found in air conditioners, washers, dryers, industrial machinery, fans, compressors, tools, blowers, vacuum cleaners, household appliances and many other applications. The reduction in the cost of the power electronic circuitry provides economically justifiable applications for adjustable speed Two-Phase Induction Motor Drives (TPIMD). In recent years, several methods that use inverters for the variable speed control of TPIM have been proposed [1]-[15]. An alternative approach is to use a 6 switch three phase Voltage-Source Inverter (VSI) bridge, connecting the two windings of the motor as an unbalanced load between the phases, as shown in Fig. 3. This is a more cost effective solution [1], [2], [9], [11], [16]. Recently, Stator Field Oriented Control (SFOC) of TPIMD has been gaining wide attention in literature [1]-[3]. In vector control, the flux linkage magnitude and the electromagnetic torque are controlled independently [14]-[15]. The SFOC represents a better solution to satisfy the industrial requirements. The field orientation is relatively straightforward in all operating conditions if the rotor speed is accurately known, which traditionally necessitates a sensor on the shaft of the motor. However, there are several reasons for preferring a system without the sensor. The cost of the speed sensor, at least for machines with ratings less than 10 kW, is in the same range as the cost of the motor itself. The

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**Corresponding author
mounting of the sensor to the motor is also an obstacle in many applications. A Sensorless system where
the speed is estimated instead of measured would essentially reduce the cost and complexity of the drive
system. In the existing literature, some approaches have been suggested for speed Sensorless single-phase
induction motor in [2], [3], [15], [17], [18], [19] and [20]. In papers [2] and [3], the authors proposed a
method of rotor speed estimation based only on the measurement of the main and auxiliary windings stator
currents and that of a reference q-axis current generated by the control algorithm. In [20], the authors
suggested to estimate the motor speed using rotor voltage vector which is defined in complex domain. In
this paper, for the first time, a speed estimation method is introduced for TPIMs based on the Model
Reference Adaptive System (MRAS) to overcome the problems of system complexity and cost. The
Sensorless speed control strategy using MRAS techniques is based on the comparison between the outputs
of two estimators when motor currents and voltages must still be measured [21], [22]. In this paper we
focus on a real implementation using DS1104 controller board of Indirect Stator Field Oriented Control
(ISFOC) of a TPIM supplied by Proportional plus Integral (PI) current controlled inverter. Our
contribution is real time implementation of a Sensorless speed control using the MRAS approach.
Simulation and experimental results are presented to demonstrate the main characteristics of the proposed
drive system. The Sensorless speed control algorithm is employed in this work and is implemented at
rated, low, and zero speed operations

2. TWO-PHASE INDUCTION MOTOR MODEL

The set of equations that defines the dynamic model for TPIM in a stationary reference frame is given by:

\[ v_{sa} = R_{sa} i_{sa} + \frac{di_{sa}}{dt} \]  \hspace{1cm} (1)

\[ v_{sb} = R_{sb} i_{sb} + \frac{di_{sb}}{dt} \]  \hspace{1cm} (2)

\[ 0 = R_{r} i_{ra} + \frac{di_{ra}}{dt} + \omega \phi_{rb} \]  \hspace{1cm} (3)

\[ 0 = R_{r} i_{rb} + \frac{di_{rb}}{dt} - \omega \phi_{ra} \]  \hspace{1cm} (4)

\[ \phi_{sa} = L_{sa} i_{sa} + M_{sar} i_{ra} \]  \hspace{1cm} (5)

\[ \phi_{sb} = L_{sb} i_{sb} + M_{sar} i_{rb} \]  \hspace{1cm} (6)

\[ \phi_{ra} = L_{r} i_{ra} + M_{sar} i_{sa} \]  \hspace{1cm} (7)

\[ \phi_{rb} = L_{r} i_{rb} + M_{sar} i_{sb} \]  \hspace{1cm} (8)

\[ T_c = n_p (M_{sar} i_{ra} - M_{sar} i_{sb}) \]  \hspace{1cm} (9)

It is seen that Eqs. (1) to (8) present the model of an asymmetrical TPIM due to the unequal resistances
and inductances of the main and auxiliary windings. This asymmetry causes an oscillating term in the
electromagnetic torque [1]. In order to simplify the mathematical model of a TPIM it is necessary, as a
first step, to introduce a transformation matrix

\[ T = \begin{bmatrix} 1 & 0 \\ 0 & k \end{bmatrix} \]

for the stator variables. Using this matrix we can write:

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\[ i_s = T_i \frac{ds_i}{dt} \tag{10} \]

\[ v_s = T_i \frac{dv_s}{dt} \tag{11} \]

\[ \phi_s = T_i \frac{d\phi_s}{dt} \tag{12} \]

where: \( k = \frac{M_{sd}}{M_{sq}} \)

Using Eqs. (1) to (12), the new mathematical model of the TPIM in a stationary reference frame can be described by the following equations:

\[ v_{sa1} = R_{sa1} i_{sa1} + \frac{d\phi_{sa1}}{dt} \tag{13} \]

\[ v_{sb1} = R_{sb1} i_{sb1} + \frac{d\phi_{sb1}}{dt} + (k^2 R_{sq} - R_{sd}) i_{sb1} \tag{14} \]

\[ 0 = R_{r} i_{ra} + \frac{d\phi_{ra}}{dt} + \omega \phi_{ra} \tag{15} \]

\[ 0 = R_{r} i_{rb} + \frac{d\phi_{rb}}{dt} - \omega \phi_{ra} \tag{16} \]

\[ \phi_{sa1} = L_{sd} i_{sa1} + M_{sd} i_{ra} \tag{17} \]

\[ \phi_{sb1} = L_{sd} i_{sb1} + M_{sd} i_{rb} + (k^2 L_{sq} - L_{sd}) i_{sb1} \tag{18} \]

\[ \phi_{ra} = L_{r} i_{ra} + M_{r} i_{sa1} \tag{19} \]

\[ \phi_{rb} = L_{r} i_{rb} + M_{r} i_{sb1} \tag{20} \]

\[ T_c = n_p M_{sd} (i_{sb1} i_{ra} - i_{sa1} i_{sb1}) \tag{21} \]

3. INDIRECT STATOR FIELD ORIENTED CONTROL (ISFOC)

Using Eqs. (17), (18) and (21), electromagnetic torque as a function of stator fluxes and stator currents can be written as:

\[ T_c = n_p (\phi_{sa1} i_{sb1} - \phi_{sb1} i_{sa1} + \Delta T) \tag{22} \]

where: \( \Delta T = (k^2 L_{sq} - L_{sd}) i_{sb1} i_{sa1} \)

In the same way, using Eqs. (15-20), we can determine the dynamic model that relates the stator flux to the stator currents:

\[ \frac{d\phi_{sa1}}{dt} + \frac{1}{\tau} \phi_{sa1} + \omega \phi_{sb1} = \frac{L_{sd}}{\tau} i_{sa1} + \sigma_d L_{sd} \frac{di_{sa1}}{dt} + \omega k^2 \sigma_d L_{sq} i_{sb1} \tag{23} \]

\[ \frac{d\phi_{sb1}}{dt} + \frac{1}{\tau} \phi_{sb1} - \omega \phi_{sa1} = k^2 \frac{L_{sq}}{\tau} i_{sb1} + k^2 \sigma_q L_{sq} \frac{di_{sb1}}{dt} - \omega \sigma_q L_{sd} i_{sa1} \tag{24} \]

in which: \( \sigma_d = 1 - \frac{M_{sd}^2}{L_{sd} L_{r}} \), \( \sigma_q = 1 - \frac{M_{sq}^2}{L_{sq} L_{r}} \), \( \tau_{sd} = \frac{L_{sd}}{R_{sd}} \), \( \tau_{sq} = \frac{L_{sq}}{R_{sq}} \) and \( \tau_r = \frac{L_r}{R_r} \).
The vector model for the stator-flux control written for an arbitrary frame (denoted by the superscript \(a\)) using Eqs. (23) and (24) are given by:

\[
\begin{align*}
\frac{d\phi_{s1}^a}{dt} + \frac{1}{\tau_r} \phi_{s1}^a + j(\omega_s - \omega)\phi_{s1}^a &= L_{sd} i_{sd1}^a + \sigma_d L_{sd} \frac{di_{sd1}^a}{dt} + j(\omega_s - \omega)\sigma_d L_{sd} i_{sd1}^a + c_s^a \\
\end{align*}
\]

(25)

where: \(\phi_{s1}^a = \phi_{s1}^a + j\phi_{s1}^a = (\phi_{s1}^a + j\phi_{s1}^a)e^{-j\delta_s}\)

\[
\begin{align*}
i_{s1}^a = i_{s1}^a + j\phi_{s1}^a = (i_{s1}^a + j\phi_{s1}^a)e^{-j\delta_s}
\end{align*}
\]

\[
\begin{align*}
\zeta_s^a &= (k^2 L_{sq} - L_{sd}) \left[ \left( \omega + \frac{1}{\tau_r} \right) i_{sq1}^a + j\frac{di_{sq1}^a}{dt} \right] e^{-j\delta_s}
\end{align*}
\]

We choose a reference frame linked to the stator flux, so that the d axis coincides with the desired direction of the stator flux (\(\phi_{adv} = \phi_{s1}^a\) and \(\phi_{avq} = 0\)). Therefore, in this synchronous rotating reference, the expression (23) can be decomposed into two equations.

\[
\begin{align*}
\frac{d\phi_{s1}^a}{dt} + \frac{1}{\tau_r} \phi_{s1}^a &= L_{sd} i_{sd1}^a + \sigma_d L_{sd} \frac{di_{sd1}^a}{dt} - \omega_s \sigma_d L_{sd} i_{sq1}^a + \zeta_d \\
\omega_s \phi_{s1} &= L_{sd} i_{sq1}^a + \sigma_d L_{sd} \frac{di_{sq1}^a}{dt} + \omega_s \sigma_d L_{sd} i_{sd1}^a + \zeta_d \\
\end{align*}
\]

(26)

(27)

where:

- \(\omega_{s1}\) : slip angular frequency;
- \(\omega_{sq}\) : synchronous angular frequency;
- \(\phi_{s1}\) : stator-flux magnitude.

It is noteworthy that the model of the stator flux (Eqs. (26) and (27)) and the expression of the torque (Eq. (22)) present additional terms (\(\zeta_d, \zeta_q\) and \(\Delta T\)) that represent the asymmetry of the machine. Note that these terms depend on \((k^2 L_{sq} - L_{sd})\). Considering that \(\zeta_d\) as well as \(\zeta_q\) and \(\Delta T\) are negligible, the model becomes symmetric and the conventional stator-field-oriented control strategy can be used [1]. If we consider that the stator flux and the electromagnetic torque are taken as control references, the following model is obtained (from Eqs. (26) and (27)):

\[
\begin{align*}
i_{sd1}^* &= \frac{\left( \tau_r p + 1 \right) \phi_{s1}^* + \tau_r \sigma_d L_{sd} i_{sq1}^* \omega_{s1}^*}{L_{sd}(1 + \sigma_d \tau_r p)} \\
i_{sq1}^* &= \frac{\phi_{s1}^* - \sigma_d L_{sd} i_{sd1}^*}{L_{sd}(1 + \sigma_d \tau_r p)}
\end{align*}
\]

(28)

(29)

4. MRAS ALGORITHM FOR SPEED ESTIMATION

a) Stator flux based MRAS speed estimation

Stator-flux based MRAS speed estimation is based on the fact that there are two ways to estimate the stator fluxes from the basic equations of the TPIM in the stationary reference frame.

- From the stator equations:
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\[
\begin{align*}
\dot{\phi}_{\alpha\alpha} &= \frac{1}{t_0} \int (v_{\alpha\alpha} - R_{s\alpha} i_{\alpha\alpha})\,dt \\
\dot{\phi}_{\beta\beta} &= \frac{1}{t_0} \int (v_{\beta\beta} - R_{s\beta} i_{\beta\beta})\,dt
\end{align*}
\]

(30)

- From the rotor equations:

\[
\begin{align*}
\dot{\phi}_{\alpha\alpha} &= \frac{\tau_r}{(1 + \tau_r p)} \left[ k \sigma_q L_{s\alpha} \omega i_{\beta\beta} + \frac{L_{s\alpha}}{\tau_r} (1 + \sigma_d \tau_r p) \dot{i}_{\alpha\alpha} - k \omega \dot{\phi}_{\beta\beta} \right] \\
\dot{\phi}_{\beta\beta} &= \frac{\tau_r}{(1 + \tau_r p)} \left[ -\frac{1}{k} \sigma_d L_{s\beta} \omega i_{\alpha\alpha} + \frac{L_{s\beta}}{\tau_r} (1 + \sigma_q \tau_r p) \dot{i}_{\beta\beta} + \frac{1}{k} \omega \dot{\phi}_{\alpha\alpha} \right]
\end{align*}
\]

(31)

Notice that the stator equations are independent of the rotor speed and are used as the reference model. The rotor equations are dependent on the rotor speed and thus can be used as the adjustable model. The system (31) leading to the so-called rotor observation is developed as:

\[
\begin{align*}
\dot{\omega} &= \frac{1}{\tau_r} \left[ -k \omega \dot{\phi}_{\beta\beta} - \frac{1}{k} \sigma_d L_{s\beta} \omega i_{\alpha\alpha} + \frac{L_{s\beta}}{\tau_r} (1 + \sigma_q \tau_r p) \dot{i}_{\beta\beta} + \frac{1}{k} \omega \dot{\phi}_{\alpha\alpha} \right] \\
\dot{\phi}_{\alpha\alpha} &= \frac{1}{\tau_r} \left[ -k \sigma_q L_{s\alpha} \omega i_{\beta\beta} + \frac{L_{s\alpha}}{\tau_r} (1 + \sigma_d \tau_r p) \dot{i}_{\alpha\alpha} - k \omega \dot{\phi}_{\beta\beta} \right] \\
\dot{\phi}_{\beta\beta} &= \frac{1}{\tau_r} \left[ -\frac{1}{k} \sigma_d L_{s\beta} \omega i_{\alpha\alpha} + \frac{L_{s\beta}}{\tau_r} (1 + \sigma_q \tau_r p) \dot{i}_{\beta\beta} + \frac{1}{k} \omega \dot{\phi}_{\alpha\alpha} \right]
\end{align*}
\]

(32)

In this paper we propose the application of MRAS to estimate the rotor speed of vector controlled TPIM by using the output error between the models of the stator flux observations (Fig. 1).

\[ \text{Reference model} \]

\[ \text{Adjustable model} \]

\[ \text{Digital Estimator System} \]

![Block scheme of MRAS for speed estimation](Fig. 1)

**b) Adaptive estimation of the rotor speed**

The main idea of the MRAS is to compare the outputs of the two models and to adjust the value of rotor speed in order to minimize the resultant error. The adjustment value is the speed generated from the error between stator fluxes observation.

The state flux error component is:

\[
p \begin{bmatrix} \dot{e}_d \\ \dot{e}_q \end{bmatrix} = \begin{bmatrix} \frac{1}{\tau_r} & -k \omega \\ \frac{1}{k \omega} & -\frac{1}{\tau_r} \end{bmatrix} \begin{bmatrix} e_d \\ e_q \end{bmatrix} + \begin{bmatrix} -k \phi_{\beta\beta} + k \sigma_q L_{s\beta} i_{\beta\beta} \\ \frac{1}{k} \phi_{\alpha\alpha} - \frac{1}{k} \sigma_d L_{s\alpha} i_{\alpha\alpha} \end{bmatrix} (\omega - \hat{\omega})
\]

(33)

where: \[ p[e] = [A][e] - [W] \]

\[ e_d = \phi_{\alpha\alpha} - \phi_{\alpha\alpha} \]
\[ \varepsilon_q = \phi_{\theta q} - \phi_{\theta r} \]
\[ \varepsilon = \begin{bmatrix} \varepsilon_d \\ \varepsilon_q \end{bmatrix} \]
\[ A = \begin{bmatrix} -\frac{1}{\tau_r} - k\omega \\ \frac{1}{k\omega} - \frac{1}{\tau_r} \end{bmatrix} \]
\[ \begin{bmatrix} W \end{bmatrix} = \begin{bmatrix} \frac{k\phi_{\theta q} - k\sigma L_{sq} \phi_{\theta r}}{k} + \frac{1}{k} \sigma L_{sd} \phi_{\theta a} \\ -\frac{1}{k} \phi_{\theta a} + \frac{1}{k} \sigma L_{sd} \phi_{\theta a} \end{bmatrix} (\omega - \ddot{\omega}) \]

Where: \([W]\) is the feedback block.

In Fig. 2, the term of \([W]\) is the input and \([\varepsilon]\) is the output of the linear feed forward block and it can be easily shown that the linear equivalent system will be completely observable and controllable. The form state Eq. (33) describes the equivalent MRAS in a linear way as it was previously specified that \([\varepsilon]\) is the main information upon which differences existing between the adjustable model and the reference model can be based.

The asymptotic behavior of the adaptation mechanism is achieved by the simplified condition \(\lim_{t \to \infty} \varepsilon = 0\) for any initialization.

\[ \int_{t_0}^{t_1} [\varepsilon]^T [W] dt \geq -\delta_0^2 \quad \text{for all} \quad t_1 \geq t_0 \quad (34) \]

where: \(\delta_0\) is a finite positive constant.

The necessary and sufficient condition for the feedback system to be hyper stable is as follows:

\(H(s) = [d - A]^{-1}\) must be a strictly positive real transfer matrix. From the previous Eq. (33) and Popov inequality, it can be easily shown that the observed speed satisfies the relationship.

\[ \ddot{\omega} = \frac{1}{p} A_1([\varepsilon]) + A_2([\varepsilon]) \quad (35) \]

with:

\[ A_1 = K_1 \left[ (\phi_{\theta q}^r \phi_{\theta a} - \phi_{\theta a}^r \phi_{\theta q}) - (i_{sa} e_q - i_{sp} e_d) \sigma L_{sq} \right] \]

\[ A_2 = K_1 \left[ (\phi_{\theta q}^r \phi_{\theta a} - \phi_{\theta a}^r \phi_{\theta q}) - (i_{sa} e_q - i_{sp} e_d) \sigma L_{sd} \right] \]
As the coefficients $K_1$ and $K_2$ of the PI regulator are involved in a non-linear system, there are no rigorous methods to compute them. Moreover, a linearization around a working point is possible, but it is preferable to find $K_1$ and $K_2$ from simulation of the complete system.

The Block diagram of speed Sensorless ISFOC for TPIM drive as illustrated in Fig. 3, where $\omega_s^*$ and $\phi_s^*$ represent the reference slip angular speed and the reference flux, respectively. The $e^{j\theta_s}$ block performs the coordinate transformation from the reference frame aligned along with the stator flux vector to the stationary reference frame.

![Block diagram of speed Sensorless ISFOC for TPIM drive](image)

**Fig. 3. Block diagram of speed Sensorless ISFOC for TPIM drive**

### 5. EXPERIMENTAL IMPLEMENTATION

To evaluate the performance of the proposed Sensorless ISFOC speed controller, the control algorithm has been implemented using a dSpace board. The dSpace works on a Matlab/Simlink platform which is a common engineering software and easy to understand and the system is controlled by software running on a dSpace DS1104 processor board. This board contains a Motorola Power PC 603e model that operates at a speed of 250 MHz and a DSP (TMS320F240 – 20 MHz). The controller is interfaced to the real system via graphical I/O-interface blocks provided by dSpace for their DS1104 hardware. Real Time Interface (RTI) is the link between dSpace real time systems and the development software Matlab/Simulink from the Math Works. It extends Real Time Workshop (C code generation) for the automatic implementation of our Simulink. The process can be commanded and monitored via the ControlDesk software of dSpace. The scheme used for the experimental setup is shown in Fig. 4.

The TPIMD is fed by a three-leg voltage source inverter (VSI) using six Insulate Bipolar Transistors (IGBT). As shown in Fig. 4, the one end of the main and auxiliary windings of the motor are connected to one half bridge each. The other ends are tied together and connected to the third half bridge. In order to reduce the ripple current of the TPIMD, a suitable PWM was implemented for the three-leg two-phase output voltages inverter. We propose sinusoidal PWM method instead of Space Vector Pulse Wide Modulation (SVPWM). In a three-leg inverter, two legs control the main and auxiliary winding of the TPIMD voltages and one leg controls the offset voltage. In the experimental test we realise PWM signals for the three leg two-phase inverter in the following way:

- PWM duty cycle is calculated according to $v_{sdref}$ for leg 1,
- PWM duty cycle is calculated according to $v_{sqref}$ for leg 2,
- Duty cycle is taken constant equal to 0.5 to provide a zero reference voltage for leg 3.
In this section, we present simulation and experimental results showing the feasibility of the proposed Sensorless speed control for TPIMD. Here, the reference flux is kept constant at the nominal value 0.8 Wb. For the speed controller an Integral-Proportional (IP) speed controller has been designed in order to stabilize the speed-control loop. The gains of the IP controller are determined using a design method to obtain a damping ratio of 1. Figure 5 shows the simulation and experimental results of the rotor speed based MRAS estimator when the machine is operating from forward zero speed to nominal speed (1500 r/min). It can be seen that at relatively nominal speed, the estimated speed tracks the actual speed reasonably well. As a second test, the starting with the reference of motor speed 1500 r/min and a step in the load torque of 5 Nm at 1s, has been performed (Fig. 6). The difference between the real and observed speeds remains very small even during the very beginning of the transient when the stator flux initialization goes up.
Fig. 6. Simulation and experimental results of sensorless ISFOC of the TPIM in the case when the speed command is 1500 r/min
Figures 6c and d show the estimated electromagnetic torque and in Fig. 6e and f the d, q components of the stator flux are estimated using the measured stator phase currents. The simulation and experimental results presented in Figs. 6c and f show that the stator fluxes converge from their initial values for their final values, respectively ($\Phi_{sd} = \Phi_{d1}$ and $\Phi_{sq} = 0$).

Using the estimated rotor speed as the feedback, the low-speed characteristics of MRAS sensorless control scheme is examined, and the results are shown in Fig. 7. The rotor speed control performance is in the low-speed operation region (30 r/min) of the rotor speed Sensorless drive. It is shown that the proposed algorithm has good speed estimation and adequate vector control characteristics at low rotor speed operation.

![Figure 7](image1)

**Fig. 7.** Simulation and experimental results of sensorless ISFOC of the TPIM for reversing speed reference from 30 r/min to -30 r/min

However, it is noticeable that the last results show clearly that the proposed MRAS scheme worked successfully for the Two-Phase Induction Motor Sensorless control algorithm.

### 6. CONCLUSION

This paper makes a contribution to the issue of sensorless ISFOC of TPIMD. Also, it presents experimental results of an efficient sensorless speed field oriented control for TPIMD. The results were satisfactory and the proposed IP controller gives the system good performances and good dynamic behaviour.

The performances of the proposed Model Reference Adaptive System (MRAS) scheme are satisfactory for both high magnitude and small transients. In this way, this technique seems promising to be transferred towards industrial applications where speed sensor is forbidden. The results presented in...
this paper show the effectiveness of observation techniques in order to remove speed sensor in vector control drives at nominal, low and zero motor speed reference controls.

**NOMENCLATURE**

\begin{align*}
& v_{sd}, v_{sq} \quad \text{d, q-axis stator voltage components} \\
& i_{sd}, i_{sq} \quad \text{d, q-axis stator current components} \\
& i_{rd}, i_{rq} \quad \text{d, q-axis rotor current components} \\
& \phi_{sd}, \phi_{sq} \quad \text{d, q-axis stator flux components} \\
& \phi_{rd}, \phi_{rq} \quad \text{d, q-axis rotor flux components} \\
& R_{sd}, R_{sq} \quad \text{stator windings resistances} \\
& R_r \quad \text{rotor resistance} \\
& L_{sd}, L_{sq} \quad \text{stator self-inductance} \\
& L_r \quad \text{rotor self-inductances} \\
& M_{sd}, M_{sq} \quad \text{mutual inductances} \\
& T_e, T_l \quad \text{electromagnetic and load torque} \\
& p = \frac{d}{dt} \quad \text{Laplace operator} \\
& \omega_s, \omega_s \quad \text{synchronous and rotor angular speed} \\
& \omega_{sl} \quad \text{slip angular speed} \left( \omega_s - \omega_r \right) \\
& \Omega \quad \text{mechanical rotor speed} \\
& n_p \quad \text{pole-pair number} \\
& f_r \quad \text{friction coefficient} \\
& J \quad \text{total inertia} \\
& \sigma_d, \sigma_q \quad \text{leakage coefficient} \\
& \tau_{sd}, \tau_{sq}, \tau_r \quad \text{stator and Rotor time constant} \\
& M. W \quad \text{main winding} \\
& A. W \quad \text{auxiliary winding} \\
& K_{pI} \quad \text{proportional gain of the IP speed controller} \\
& K_{iI} \quad \text{integral gain of the IP speed controller} \\
& K_{pI} \quad \text{proportional gain of the PI current controller} \\
& K_{iI} \quad \text{integral gain of the PI current controller} \\
& * \quad \text{reference value}
\end{align*}

**REFERENCES**


**APPENDIX**

Table A.1: Two-phase induction machine parameters

<table>
<thead>
<tr>
<th>Specification</th>
<th>Parameters</th>
</tr>
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<tbody>
<tr>
<td>Rated power</td>
<td>1.1 kW</td>
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<tr>
<td>R_sd</td>
<td>2.473 Ω</td>
</tr>
<tr>
<td>Rated voltage</td>
<td>220 V</td>
</tr>
<tr>
<td>R_sq</td>
<td>6.274Ω</td>
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<tr>
<td>Rated current</td>
<td>6.58 A</td>
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<tr>
<td>R_r</td>
<td>5.514Ω</td>
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<td>Rated frequency</td>
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<tr>
<td>L_sd</td>
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</tr>
<tr>
<td>Number of pole pairs</td>
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</tr>
<tr>
<td>L_rq</td>
<td>0.1099 H</td>
</tr>
<tr>
<td>Rated speed</td>
<td>1430 r/min</td>
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<td>L_r</td>
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<td></td>
<td>M_sd</td>
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<tr>
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