

TWO APPROACHES ON CARRIER FREQUENCY OFFSET ESTIMATION IN MIMO OFDM SYSTEMS*

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Abstract– We consider the problem of joint carrier frequency offset and channel estimation between transmitter and receiver in a frequency-selective channel MIMO-OFDM system. Recently two high performance estimators based on the expectation-maximization (EM) algorithm have been proposed. The main drawback of the maximum likelihood base algorithms, like EM algorithm, is the high computational complexity. In this paper, we propose an extended Kalman filter based estimator, which has higher performance than that of EM algorithm, while its computational complexity is lower. In addition, the Particle Swarm Optimization (PSO) algorithm is used for joint ML estimation of carrier frequency offset and channel parameters for the general model. The proposed method has a lower computational complexity than that of traditional search methods. Simulation results in comparison with Cramer-Rao bound show that the proposed algorithms outperform the EM in all ranges of signal-to-noise ratio for both channel and frequency offset estimations. Also, among them, the PSO algorithm is superior.

Keywords– Carrier frequency offset (CFO), estimation, MIMO-OFDM, extended Kalman filter (EKF), particle swarm optimization (PSO)

1. INTRODUCTION

The combination of multiple-input multiple-output (MIMO) wireless technology with orthogonal frequency division multiplexing (MIMO-OFDM) is a remedial solution for next generation wireless local area networks (WLANs), wireless metropolitan area networks (WMANs), and fourth-generation mobile cellular wireless systems. Since OFDM offers the possibility for high data rates at low decoding complexity, it has been widely adopted by many standards (e.g., IEEE802.11a, IEEE802.11g in the U.S., and digital audio/video broadcasting (DAB/DVB), HiperLAN/2 in Europe) [1, 2], although OFDM is a promising technique, especially when we combine it with spatial diversity techniques, i.e., MIMO systems in more general case, its high sensitivity to carrier frequency offset (CFO) due a difference between the carrier frequencies of the local oscillators at the transmitter and the receiver, produces inter carrier interferences (ICI) and causes desired signal attenuation, and as such introduces a huge performance loss.

Whereas OFDM is robust to the multipath delay, in order to achieve high-quality transmission [3] and avoid phase and amplitude distortion due to coherent detection and decoding in fading channel, the estimation of channel parameters and compensation is necessary in addition to the frequency offset estimation. Joint estimation of CFO and channel impulse response (CIR) parameters leads to particularly complex problems because of the number of unknowns [4]. A number of approaches have dealt with the CFO and channel estimation in a single-input single-output (SISO) OFDM setup in literature [5, 6]. Although the CFO estimation is a well studied problem in the SISO systems, it is relatively novel for the

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MIMO-OFDM systems. In SISO OFDM, some methods rely on training blocks [7, 8], while others just take advantage of standard transmission format; e.g., exploit the presence of null sub-carriers and save the transmission bandwidth by blind estimation [9, 10]. In order to obtain the maximum-likelihood (ML) estimation of CFO, the prohibitive computational complexity is required [11]. Saemi et al. in [12, 13] have proposed a new algorithm for time-frequency synchronization joint with the channel identification in MIMO-OFDM systems. The high complexity is one drawback of this method. Salari et al. in [14] have proposed a ML solution in an iterative manner; e.g., expectation-maximization (EM) algorithm [15]. Their CFO estimator first provides a CIR estimate in the expectation (E)-step and then estimates the CFO in the maximization step (M)-step. Because of the estimator complexity, they have also proposed a simpler estimator with a decrease in performance.

The Extended Kalman Filter (EKF) has been widely used for estimation in non-linear systems [16]. In this paper, we propose a CFO estimator based on the EKF whose complexity is less than that of ML estimator, although its performance is better. Moreover, according to the Particle Swarm Optimization (PSO) theory, a joint ML estimation algorithm of CFO and channel for the general model is proposed. The advantages of the proposed algorithm are that it is simple in conception, easy to implement, and efficient in computation. The PSO-based estimation algorithm has a lower computational complexity than that of traditional search methods. This makes the computational efficiency of the mentioned method higher.

The rest of the paper is organized as follows: The next section contains an introduction to MIMO-OFDM system model which experiences carrier frequency offset. Section III briefly explains the ML, EM, and proposed algorithms. This paper ends with the simulation results and conclusion in section IV and V.

2. MIMO-OFDM SYSTEM MODEL

A discrete-time FFT/IFFT-based $N_t \times N_r$ MIMO-OFDM system is considered and its typical structure as a block diagram is shown in Fig.1. The time-domain complex baseband samples $\{\mathbf{s}_j\}, j=1, \dots, N_t$ with N_c subcarriers are generated by taking N_c -point inverse fast Fourier transform $\{\text{IFFT}_{N_c}\}$ of a block of subcarrier symbols $\{\mathbf{X}_j\}$. Then we construct $\{\mathbf{u}_j\}, j=1, \dots, N_c + N_g$ by adding a cyclic prefix with length N_g preceding each symbol, which should be longer than the CIR length (L), so that there will be no inter-symbol interference (ISI). Then the baseband signal is up-converted to the radio frequency (RF) f_c after parallel-to-serial (P/S) conversion, and transmitted through the N_t transmit antennas. The channel is a Rayleigh frequency-selective fading which is described by complex Gaussian matrix elements. Also, it is assumed that the fading process remains static during each OFDM word (one time slot) and varies from one OFDM block to another. The fading processes associated with different transmitter-receiver antenna pairs are uncorrelated. At each receive antenna, a superposition of faded signal plus noise is received. Received signals are down-converted to baseband with the local oscillators centered at \hat{f}_c . The samples at the i^{th} receive antenna filter can be written as [14]

$$r_i(k) = \exp\left\{j\frac{2\pi\varepsilon}{N_c}k\right\} \sum_{j=1}^{N_t} \sum_{l=0}^{L-1} h_{i,j}(l) \cdot u_j(k-l) + v_i(k), \quad i=1,2,\dots,N_r \quad (1)$$

where $h_{i,j}(l)$ is the l^{th} element of the CIR between the j^{th} transmitter and the i^{th} receiver,

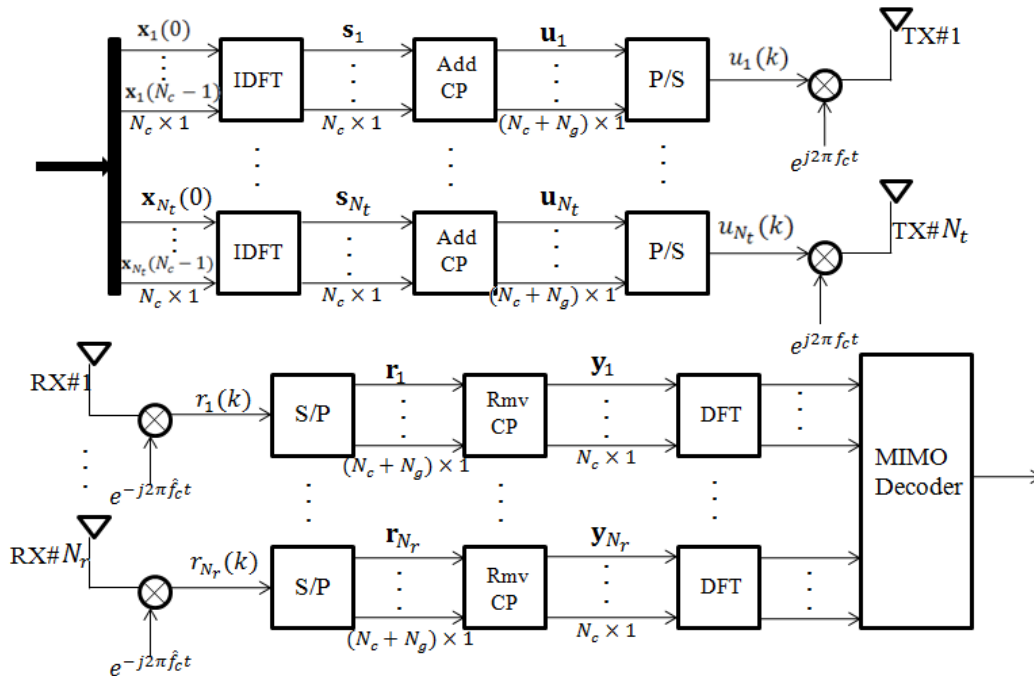


Fig. 1. Transmitter-receiver structure of a $N_t \times N_r$ MIMO-OFDM system [14]

$u_j(k)$ is the sample of \mathbf{u}_j after P/S in time k , ε is the CFO normalized to the subcarrier spacing $1/T$ and $v_i(k)$ is the channel noise sample that is an additive white complex Gaussian noise with zero mean and variance $\sigma_{v_i}^2$. After serial-to-parallel (S/P) conversion and removing the cyclic prefix, we will reach \mathbf{y}_i in the i^{th} receiver as

$$\mathbf{y}_i = \exp\left\{j\frac{2\pi\varepsilon}{N_c}N_g\right\} \sum_{j=1}^{N_t} \mathbf{F}(\varepsilon) \cdot \mathbf{A}_j \cdot \mathbf{h}_{i,j} + \mathbf{v}_i, \quad i = 1, 2, \dots, N_r \quad (2)$$

where

$$\mathbf{F}(\varepsilon) = \text{diag}\left\{1, \exp\left\{j\frac{2\pi\varepsilon}{N_c}\right\}, \dots, \exp\left\{j\frac{2\pi\varepsilon}{N_c}(N_c - 1)\right\}\right\}_{N_c \times N_c}, \quad (3)$$

$$[\mathbf{A}_j]_{a,b} = s_j\left[|a - b|_{N_c}\right], \quad 1 \leq a \leq N_c, 1 \leq b \leq L, \quad (4)$$

and $\mathbf{h}_{i,j} = [h_{i,j}(0), \dots, h_{i,j}(L-1)]^T$, $1 \leq j \leq N_t, 1 \leq i \leq N_r$ describes the L order realization of the channel between the j^{th} transmitter and the i^{th} receiver. The random vectors $\mathbf{h}_{i,j}$ are assumed to be independent with zero mean complex Gaussian distribution. $s_j(p)$ denotes the p^{th} entry of \mathbf{s}_j for $1 \leq p \leq N_c$ and $|q|_K$ denotes the modulo- K of q that is located in the interval $[0, K-1]$, indeed \mathbf{A}_j is in the form (5) to implement the convolution operator.

$$\mathbf{A}_j = \begin{bmatrix} s_j(0) & s_j(N_c - 1) & \dots & s_j(N_c - L + 1) \\ s_j(1) & s_j(0) & \dots & s_j(N_c - L + 2) \\ \vdots & \vdots & \ddots & \vdots \\ s_j(N_c - 1) & s_j(N_c - 2) & \dots & s_j(N_c - L) \end{bmatrix}. \quad (5)$$

The vector \mathbf{v}_i containing the channel noise samples $v_i(k)$, is complex Gaussian with zero mean and covariance matrix $\sigma_{v_i}^2 \mathbf{I}$. We can simplify the input-output equation (2) by rewriting it in matrix form as

$$\mathbf{y}_i = \mathbf{F}(\varepsilon) \cdot \mathbf{A}(\varepsilon) \cdot \mathbf{h}_i + \mathbf{v}_i, \quad i = 1, \dots, N_r \quad (6)$$

where

$$\mathbf{A}(\varepsilon) = \left[\exp\left\{j \frac{2\pi\varepsilon}{K} N_g\right\} \mathbf{A}_1, \dots, \exp\left\{j \frac{2\pi\varepsilon}{K} N_g\right\} \mathbf{A}_{N_t} \right]_{N_c \times N_t \cdot L} \quad (7)$$

$$\mathbf{h}_i = \left[\mathbf{h}_{i,1}^T, \mathbf{h}_{i,2}^T, \dots, \mathbf{h}_{i,N_t}^T \right]_{N_t \cdot L \times 1}^T \quad (8)$$

Here, the channel and noise are assumed to be statistically independent.

3. JOINT CFO AND CIR ESTIMATION

a) ML estimation and EM algorithm

The transmission model has two unknown parameters: the normalized CFO, ε , and the coefficients of CIR, \mathbf{h}_i ($i = 1, \dots, N_r$). Based on the signal model in (6), the ML estimation of parameters $\{\varepsilon, \mathbf{h}_i\}$ is given by maximizing the likelihood function that is equivalent to minimizing the cost function shown below:

$$\min_{\varepsilon, \mathbf{h}_i} \left\{ \sum_{i=1}^{N_r} \frac{1}{\sigma_{v_i}^2} \left\| \mathbf{y}_i - \mathbf{F}(\varepsilon) \mathbf{A}(\varepsilon) \mathbf{h}_i \right\|^2 \right\} \quad (9)$$

First, assuming the CFO to be fixed and because of independence between \mathbf{h}_i s the ML estimate of \mathbf{h}_i is obtained as

$$\hat{\mathbf{h}}_i = \left(\mathbf{A}(\varepsilon)^H \mathbf{A}(\varepsilon) \right)^{-1} \mathbf{A}(\varepsilon)^H \mathbf{F}(\varepsilon)^H \mathbf{y}_i, \quad i = 1, \dots, N_r \quad (10)$$

Then substituting $\hat{\mathbf{h}}_i$ into (9) and after some manipulation, we obtain the estimation of ε as

$$\hat{\varepsilon} = \arg \max_{\varepsilon} \left\{ \sum_{i=1}^{N_r} \frac{1}{\sigma_{v_i}^2} \left\| \mathbf{A}(\varepsilon) \left(\mathbf{A}(\varepsilon)^H \mathbf{A}(\varepsilon) \right)^{-1} \mathbf{A}(\varepsilon)^H \mathbf{F}(\varepsilon)^H \mathbf{y}_i \right\|^2 \right\} \quad (11)$$

The above ML estimation method of CFO requires a huge computational search over the trial values of CFO. Although the accuracy of ML estimation is high, this computational complexity makes a serious challenge in the practical applications.

To circumvent this problem, Salari et al. in [14] have used the EM algorithm. In [14], the CIR parameters are obtained in the expectation step and the CFO is estimated in maximization step. They have also formed a computationally simpler CFO estimator with a slight loss. In this paper, we consider the first estimator of [14] as EM algorithm which is called EM.

b) Extended Kalman filter

The EKF is a recursive algorithm composed of two stages named time and measurement update stages. If the state model is

$$\mathbf{x}_n = f(\mathbf{x}_{n-1}) + \mathbf{w}_{n-1} \quad (12)$$

$$\mathbf{y}_n = \Gamma(\mathbf{x}_n) + \mathbf{v}_n \quad (13)$$

where \mathbf{x}_n , \mathbf{y}_n , \mathbf{w}_{n-1} , and \mathbf{v}_n are the state vector, observation vector, state noise and measurement noise respectively, these two stages are presented by the following equations:

Time Update Equations:

$$\hat{\mathbf{x}}_{n|n-1} = f\left(\hat{\mathbf{x}}_{n-1|n-1}\right) \quad (14)$$

$$\mathbf{P}_{n|n-1} = \mathbf{F}_{n-1}\mathbf{P}_{n-1|n-1}\mathbf{F}_{n-1}^T + \mathbf{Q}_{n-1} \quad (15)$$

Measurement Update Equations:

$$\hat{\mathbf{x}}_{n|n} = \hat{\mathbf{x}}_{n|n-1} + \mathbf{K}_n \left(\mathbf{y}_n - \Gamma\left(\hat{\mathbf{x}}_{n|n-1}\right) \right) \quad (16)$$

$$\mathbf{K}_n = \mathbf{P}_{n|n-1}\mathbf{H}_n^T \left(\mathbf{H}_n\mathbf{P}_{n|n-1}\mathbf{H}_n^T + \mathbf{R}_n \right)^{-1} \quad (17)$$

$$\mathbf{P}_{n|n} = (\mathbf{I} - \mathbf{K}_n\mathbf{H}_n)\mathbf{P}_{n|n-1} \quad (18)$$

where $\hat{\mathbf{x}}_{n|n-1}$ and $\mathbf{P}_{n|n-1}$ are the predicted state and estimate covariance respectively, $\hat{\mathbf{x}}_{n|n}$ and $\mathbf{P}_{n|n}$ are the updated state and estimate covariance from the data until time n respectively, and $\mathbf{F}_n = \left. \frac{\partial f}{\partial \mathbf{x}} \right|_{\hat{\mathbf{x}}_{n|n}}$

and $\mathbf{H}_n = \left. \frac{\partial \Gamma}{\partial \mathbf{x}} \right|_{\hat{\mathbf{x}}_{n|n-1}}$. Also, \mathbf{K}_n is the Kalman gain, \mathbf{R}_n and \mathbf{Q}_n are the measurement and state noise

covariance matrices and n is the number of EKF updating step. When \mathbf{R}_n and \mathbf{Q}_n are unknown, they can be ML estimated during execution of the EKF steps from the equations below:

$$\mathbf{R}_n = \frac{1}{M} \sum_{l=n-M}^{n-1} \hat{\mathbf{v}}_l \hat{\mathbf{v}}_l^H \quad (19)$$

$$\mathbf{Q}_n = \frac{1}{M} \sum_{l=n-M}^{n-1} \hat{\mathbf{w}}_l \hat{\mathbf{w}}_l^H \quad (20)$$

where $\hat{\mathbf{v}}_l = \mathbf{y}_l - \Gamma\left(\hat{\mathbf{x}}_{l|l-1}\right)$ and $\hat{\mathbf{w}}_l = \hat{\mathbf{x}}_{l|l} - f\left(\hat{\mathbf{x}}_{l-1|l-1}\right)$, and M is the number of estimated noise vectors in the ML estimation.

The time update equations are responsible for projecting forward (in time) the current state and error covariance estimates to obtain the apriori estimates for the time step. The measurement update equations are responsible for the feedback, i.e., for incorporating a new data into apriori estimate to obtain an improved aposteriori estimate. The time update equations can also be thought of as predictor equations, while the measurement update equations can be thought of as corrector equations.

If we consider ε as the state variable in our problem, the linear state-variable model can be written as follows:

$$\varepsilon_{n+1} = \varepsilon_n + w_n \quad (21)$$

where the state noise w_n is assumed to be an additive white complex Gaussian noise with zero mean and unknown variance $\sigma_{w_n}^2$. Notice that in this model, state variable \mathbf{x}_n and state noise \mathbf{w}_{n-1} are scalar (denoted as ε_n and w_n respectively). The measurement equation (observation vector) can be reformulated as

$$\mathbf{y}_n = \Gamma(\varepsilon_n) + \mathbf{v}_n \quad (22)$$

where the nonlinear function $\Gamma(\cdot)$ of the state variable ε_n is defined as $\Gamma(\varepsilon_n) = \mathbf{F}(\varepsilon_n)\mathbf{A}(\hat{\varepsilon})\hat{\mathbf{h}}_i$. Consider that $\mathbf{A}(\hat{\varepsilon})$ has been computed by (7) for $\hat{\varepsilon} = \hat{\varepsilon}_{n|n-1}$ and $\hat{\mathbf{h}}_i$ has already been estimated by an ML solution as $\hat{\mathbf{h}}_i = \left[\mathbf{A}(\hat{\varepsilon})^H \mathbf{A}(\hat{\varepsilon}) \right]^{-1} \mathbf{A}(\hat{\varepsilon})^H \mathbf{F}(\hat{\varepsilon})^H \mathbf{y}_i$, like the E-step of the EM algorithm in [14].

Since the observation equation is a nonlinear function of the CFO, an EKF-based algorithm is used to estimate the CFO. Let $\hat{\varepsilon}_{n|n-1}$ be our apriori state estimation at step n , given knowledge of the process prior to the step n , $\hat{\varepsilon}_{n|n}$ be our aposteriori state estimation at step n given data \mathbf{y}_n and $\mathbf{P}_{n|n-1}$ and $\mathbf{P}_{n|n}$ are apriori and aposteriori error estimation covariance respectively.

c) Proposed CFO estimation algorithm

In the proposed EKF algorithm, N_r data streams (each stream contains N_c samples) are used to estimate the CFO. Each data stream per receive antenna is consecutively used for one updating step of EKF procedure; in other words, here, the number of EKF updating step n is the number of receive antenna. Since the number of receivers is not a lot, to improve the EKF algorithm, we propose an iterative procedure. In this method, after updating the CFO during N_r updating steps using data from the first receive antenna to the last receive antenna, the estimated CFO of EKF is fed back to the EKF algorithm as an initial CFO ($\hat{\varepsilon}_{1|0}$), and the EKF algorithm is again repeated by the new initial value. In the new iteration; $\mathbf{P}_{1|0}$ is also substituted from the previous iteration. Although the $N_r \times N_c$ data symbols are the same in the different iterations, $\hat{\varepsilon}$ and P improve during each iteration because of passing the transient state. Due to the iterative nature of this algorithm, we call it Iterative Extended Kalman Filter (IEKF). This iterative procedure can be continued until the rational mean square error (MSE) is achieved.

d) Particle swarm optimization algorithm

Particle Swarm Optimization, inspired by the social behavior of swarms of birds and fish schools, is a high performance optimizer first presented by Eberhart and Kennedy [17]. Compared to the conventional optimization techniques such as the Genetic Algorithms (GA), the PSO benefits from its algorithmic simplicity and robustness. The PSO exploits a swarm of particles which seek the promising regions of the D-dimension search space with adaptable velocity. Each particle changes its position based on its encountered best position and the best position attained by all particles.

Consider m particles with position and velocity vectors as \mathbf{x}_i and \mathbf{v}_i , $i = 1, 2, \dots, m$ respectively. The equations of updating the velocity and position in the PSO are stated by (23) and (24) as

$$v_{i,j}^{(k+1)} = w^{(k)} v_{i,j}^{(k)} + c_1 r_1 \left(pbest_{i,j}^{(k)} - x_{i,j}^{(k)} \right) + c_2 r_2 \left(gbest_j^{(k)} - x_{i,j}^{(k)} \right) \quad (23)$$

$$x_{i,j}^{(k+1)} = x_{i,j}^{(k)} + v_{i,j}^{(k+1)}, \quad i = 1, \dots, m, \quad j = 1, \dots, J \quad (24)$$

where

- $v_{i,j}^{(k)}$ is the j^{th} component of velocity vector of particle i at iteration k .
- $v_{i,j}^{(k+1)}$ is the j^{th} component of modified velocity vector of particle i at next iteration $k+1$.
- $x_{i,j}^{(k)}$ is the j^{th} component of position vector of particle i at iteration k .
- $x_{i,j}^{(k+1)}$ is the j^{th} component of the modified position of particle i at next iteration $k+1$.
- r_1, r_2 are random numbers between 0 and 1 (representing the random movement of each particle).
- $pbest_{i,j}^{(k)}$ is the j^{th} component of $\mathbf{pbest}_i^{(k)}$ which is the best position found by the particle i at iteration k .
- $gbest_j^{(k)}$ is the j^{th} component of $\mathbf{gbest}^{(k)}$ which is the best position found by the particle swarm separately at iteration k .
- c_1, c_2 are positive constants (weigh the influence of individual and social learning, respectively).
- $w^{(k)}$ is inertia weight at iteration k .

The inertia weight factor w balances the ability of exploration (global search) and exploitation (local search). In general, the large value of w is prone to global region hunting and the small value of w helps local region probing. Linearly decreasing inertia weights were recommended in [18] and PSO with decreasing inertia weights has better performance. The mentioned inertia weight is as follows

$$w^{(k)} = w_{\max} - \frac{w_{\max} - w_{\min}}{k_{\max}} \times k, \quad k = 1, 2, \dots, k_{\max} \quad (25)$$

where w_{\min} and w_{\max} represent the range of inertia weight and k_{\max} is the maximum iteration number.

In general, the PSO algorithm can be described as follows:

- 1) Initialize each particle i of the population by randomly selecting values for its location $\mathbf{x}_i^{(k)}$ and velocity $\mathbf{v}_i^{(k)}$ vectors.
- 2) Calculate the fitness value of each particle. If the current fitness value for the particle is greater than the best fitness value found for the particle so far, then $\mathbf{pbest}_i^{(k)}$ is updated.
- 3) Determine the location of the particle with the highest fitness and update $\mathbf{gbest}^{(k)}$ if necessary.
- 4) For each particle, calculate the velocity according to the equation (23).
- 5) Update the position of each particle according to the equation (24).
- 6) Repeat steps 2-5 until reaching the termination condition (number of iterations or precision).

Before employing the PSO method to solve the CFO estimation, two definitions must be made as follows: 1) Representation of the particle. The particle is the CFO (ε) in our problem, 2) Determination of the fitness function. According to (11), the fitness function is

$$FIT = \sum_{i=1}^{N_r} \frac{1}{\sigma_{v_i}^2} \left\| \mathbf{A}(\varepsilon) \left(\mathbf{A}(\varepsilon)^H \mathbf{A}(\varepsilon) \right)^{-1} \mathbf{A}(\varepsilon)^H \mathbf{F}(\varepsilon)^H \mathbf{y}_i \right\|^2 \quad (26)$$

4. SIMULATION RESULTS

In this section, we present the results of simulations to demonstrate the effectiveness of the proposed schemes. The system parameters are presented in Table 1 which are held constant throughout the simulations. The data symbols are complex independent and identically distributed from 4-QAM constellation with $\sigma_x^2 = 1$. The signal-to-noise-ratio (SNR) is defined as $SNR = E_x / \sigma_v^2$ where E_x is the total transmitted signal energy and σ_v^2 is the variance of channel noise corresponding to each receiver. Given the parameters in Table 1, the simulations have been executed with 1000 Monte Carlo iterations. We have also used $\hat{\varepsilon}_{1|0} = 0$ and $\mathbf{P}_{1|0} = \mathbf{I}$ for IEKF initialization and assumed known $\mathbf{R}_0 = \sigma_v^2 \mathbf{I}_{N_c \times N_c}$ equal to noise covariance for each receive antenna.

Table 1. System settings in simulations

Number of carriers	128
Channel power delay profile (PDP)	[0.55,0.24,0.11,0.04,0.02]
Guard time (Cyclic Prefix)	5 symbol period
Modulation	4-QAM

In the simulation of the PSO algorithm c_1 and c_2 are set to 1.49 [19], w_{\max} (w in start) and w_{\min} (w in end) are 0.64 and 0.4, k_{\max} and swarm size (m) are equal to 20 and 16 respectively.

For performance evaluation, the MSE of the normalized CFO estimation i.e. $E\left\{\|\varepsilon - \hat{\varepsilon}\|^2\right\}$ is applied.

We also use the MSE as $E\left\{\|\mathbf{h} - \hat{\mathbf{h}}\|^2\right\}$ for channel estimation evaluation, where $\mathbf{h} = [\mathbf{h}_1^T, \mathbf{h}_2^T, \dots, \mathbf{h}_{N_r}^T]^T$.

a) Performance evaluation of the proposed algorithms

We first consider four 2×2 , 3×3 , 4×4 and 6×6 MIMO-OFDM systems in the simulation and the CFO is set as $\varepsilon = 0.1$. Fig. 2 and Fig. 3 depict the MSE of CFO estimation versus SNR for the IEKF and PSO methods respectively. Here, SNR is varied from 0 to 30 dB over a frequency-selective fading channel. From Fig. 2 and Fig. 3, it can be observed that the performance of both algorithms is satisfactory even in low SNR and small number of antennas. Also, as predicted, by increasing SNR or the number of transmit-receive antennas, their performance improves.

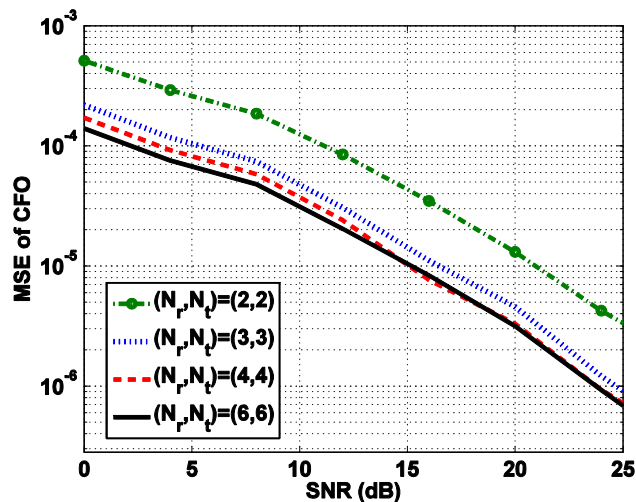


Fig. 2. MSE of CFO estimation by IEKF versus SNR for different number of transmit-receive antennas in $\varepsilon = 0.1$

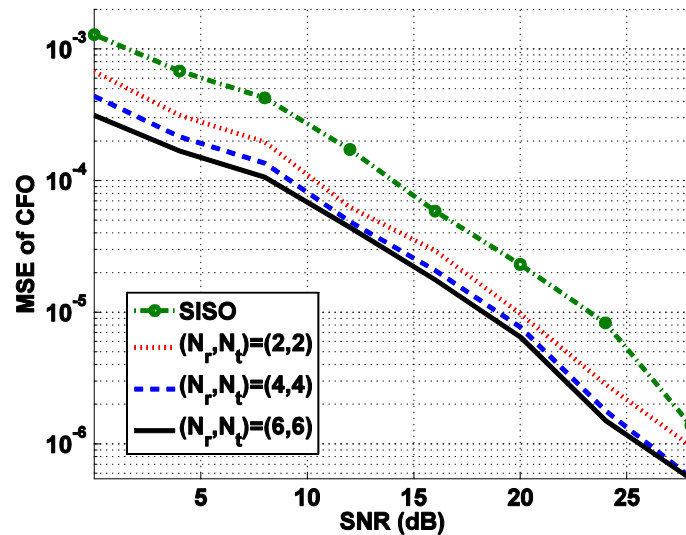


Fig. 3. MSE of CFO estimation by PSO versus SNR for different number of transmit-receive antennas in $\varepsilon = 0.1$

Then, for performance comparison, we consider a 2×2 MIMO-OFDM system and set the CFO as $\varepsilon = 0.06$. In Fig. 4, the MSE of CFO versus SNR for IEKF and PSO methods is compared to that of EM method and Cramer Rao Bound (CRB) [14. Eq. (27)]. It can be found that while the performance of the IEKF algorithm is better than that of EM, the PSO outperforms both of them and is closer to the CRB. The main point is the huge complexity reduction in the IEKF algorithm compared to the EM algorithm. Furthermore, it is noticeable that the performance of the IEKF algorithm and PSO method is more improved when the SNR increases.

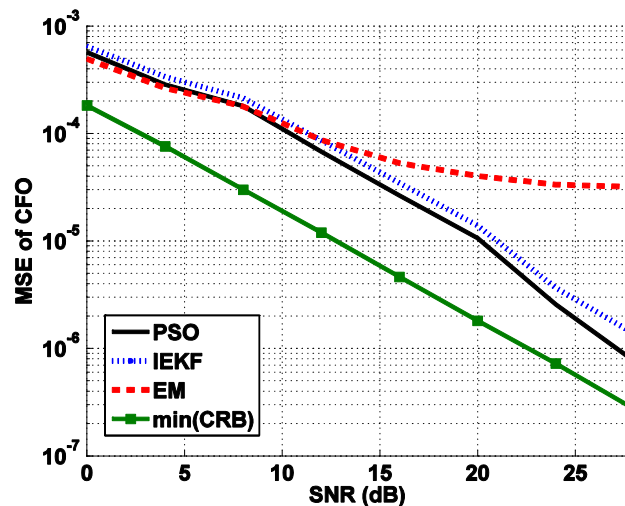


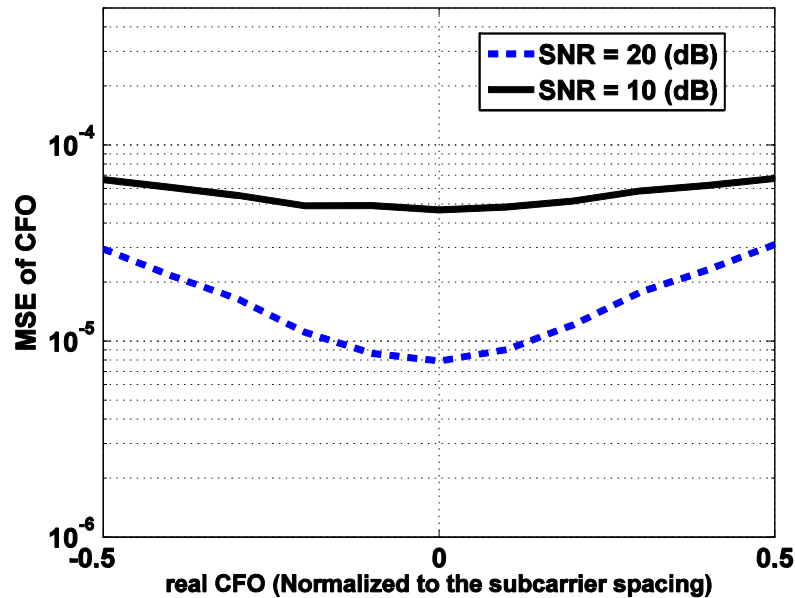
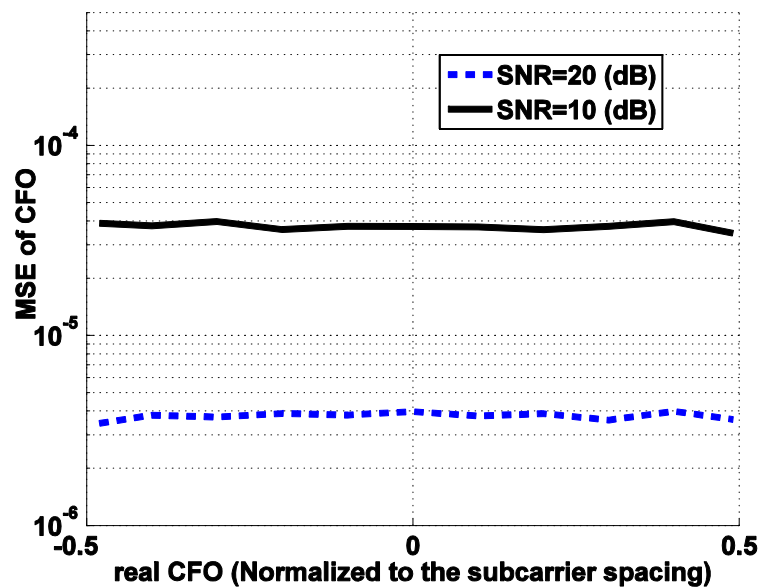
Fig. 4. Comparison between the accuracy of the proposed CFO estimators with that of EM method and CRB in $\varepsilon = 0.06$

We have chosen simulation time to evaluate the computational complexity of proposed methods in comparison with the EM method. The algorithms have run using Intel(R) Core(TM) 2 Duo CPU. The number of iterations in both EM and IEKF algorithms is 10. Each method has run 100 times and the average execution times of simulations are presented in Table 2. As seen from the table, the IEKF algorithm has the lowest complexity compared to the other algorithms. The EM algorithm has the most complexity.

Table 2. Average execution times of the proposed methods in comparison with the EM method

Estimation Method	Execution Time (sec)
EM	3.34
IEKF	0.09
PSO	0.57

For evaluating the performance of the proposed algorithms in various values of real CFO, we present the MSE of CFO estimation curves versus the real CFO (ε). Figures 5 and 6 show these curves for two different values of SNR for the IEKF and PSO method respectively.

Fig. 5. MSE of CFO estimation by IEKF versus real CFO (ε) for two different values of SNRFig. 6. MSE of CFO estimation by PSO versus real CFO (ε) for two different values of SNR

Consider that the CFO has been normalized to the subcarrier spacing. The algorithms have been run with 1000 iterations for each frequency offset in SNR equal to 10 or 20 dB. As can be seen, from these

figures, the previous results according to some selected values of CFO can be generalized to all values of CFO. However, the MSE of CFO estimation in the IEKF method becomes less for smaller real CFO. It is clear that the acquisition range of the proposed algorithms is at least equal to one subcarrier spacing.

b) Performance of IEKF for different number of iteration

The number of iteration is an important parameter in the IEKF algorithm. In Fig. 7, we evaluate the effect of number of iteration in the IEKF algorithm. The MSE performance has been obtained for a 2×2 MIMO-OFDM system and the CFO has been fixed on 0.1. It is obvious that increasing the number of iterations improves the performance of the algorithm; nonetheless, what is significant is that with more than 10 iterations, the perfect performance is almost provided. Thus, in the related simulations, we have set the IEKF iterations to 10.

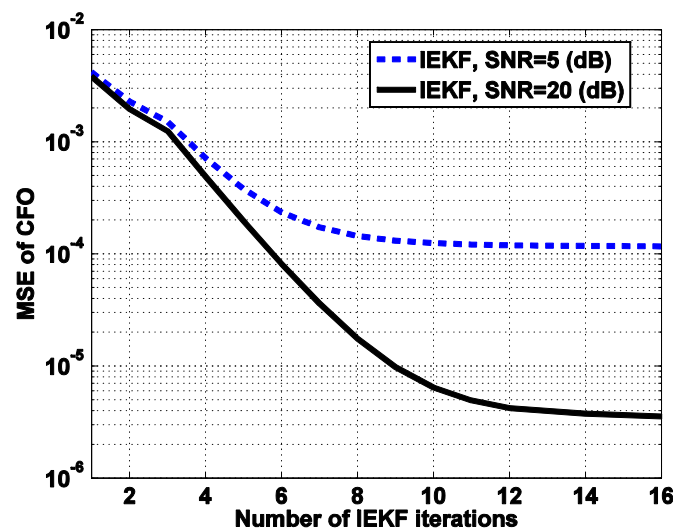


Fig. 7. MSE of CFO estimation by IEKF versus the number of iterations for two different values of SNR

c) Investigating on the selection of parameters of PSO algorithm

In Figs. 8, 9, and 10, we illustrate the effect of inertia weight (ω), maximum iteration number (k_{\max}) and swarm size (m) in the performance of PSO algorithm respectively. The MSE performance has been obtained for a 2×2 MIMO-OFDM system with CFO equal to 0.2. As shown in Fig. 8, changing the interval of inertia weight has little effect on the performance of PSO algorithm. Also, regarding Figs. 9 and 10, it is concluded that a choice larger than 10 for k_{\max} and equal to 15 for the swarm size is suitable for getting an appropriate performance.

d) Performance of estimation of CIR

In the proposed algorithms, we also estimate the CIR simultaneously. Figure 11 depicts the MSE of CIR estimation versus SNR for IEKF and PSO methods in comparison with that of EM method and ideal case (with perfectly known CFO). The MIMO-OFDM system has been considered as 2×2 and the real CFO is $\varepsilon = 0.06$. This comparison demonstrates that the ML CIR estimator used in the proposed algorithms tends to the ideal bound, while the EM estimator deviates from them for large SNR.

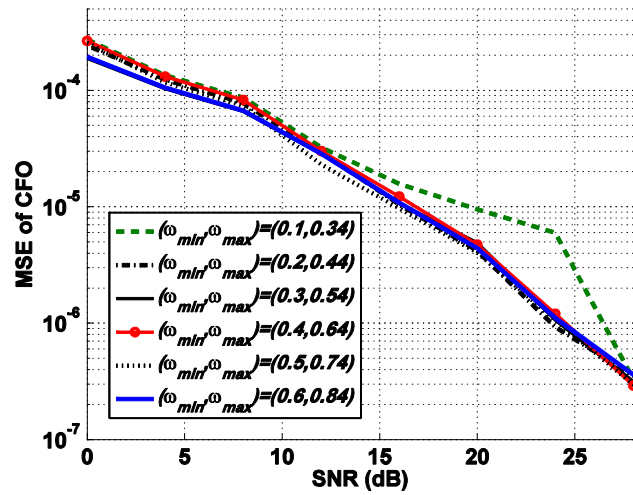


Fig. 8. Investigation of the effect of inertia weight in PSO algorithm by using various interval (w_{end}, w_{start}) in $\epsilon=0.2$

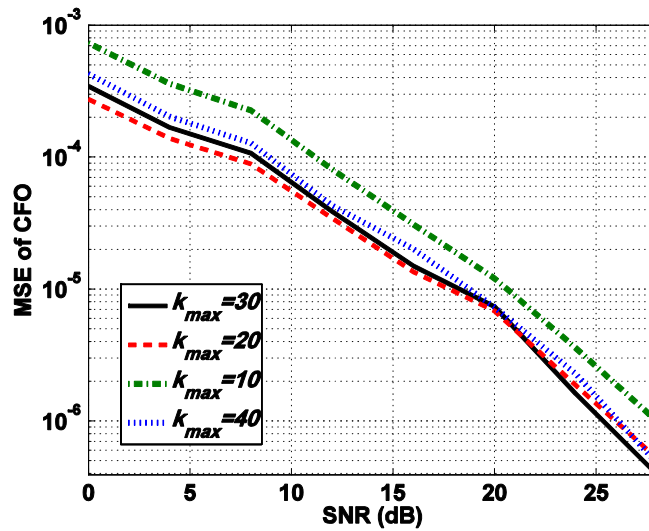


Fig. 9. Investigation of the effect of iteration number in PSO algorithm

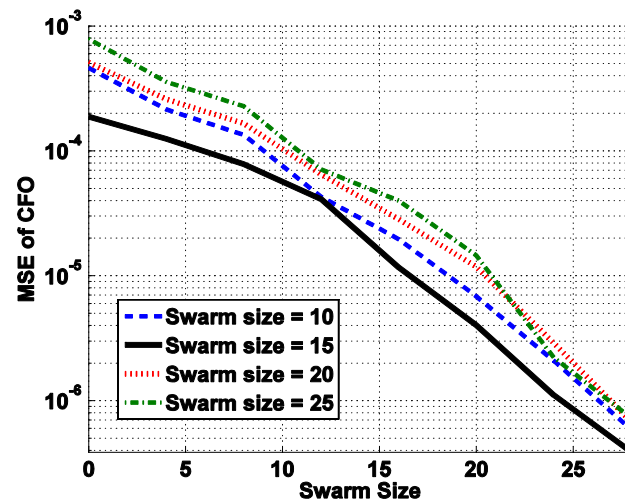


Fig. 10. Investigation of the effect of Swarm size in PSO algorithm

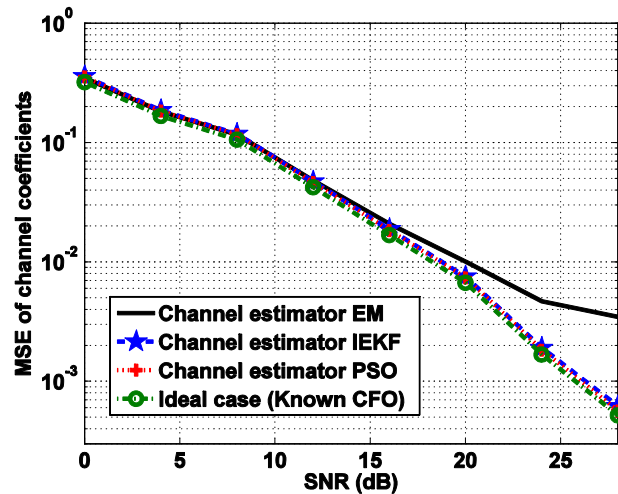


Fig. 11. The MSE performance of proposed methods in channel estimation in comparison with that of EM method and ideal case in $\epsilon=0.06$

5. CONCLUSION

In this paper, we proposed a novel iterative carrier frequency offset estimation algorithm based on the EKF algorithm and multi-antenna channel ML estimation for MIMO-OFDM systems. In the proposed scheme, we implement the EKF updating steps on the number of receive antennas and, after each cycle, the last estimated CFO of EKF is fed back to the estimator iteratively. The PSO algorithm was also used for CFO ML estimation. The proposed algorithms not only outperform the EM algorithm, but also have much lower computational complexity. The performance of our estimators was investigated by computer simulations and benchmarked with CRB. Simulation results show that the accuracy of the proposed algorithms is close to the CRB.

NOMENCLATURE

MIMO	multiple-input multiple-output
OFDM	orthogonal frequency division multiplexing
WLANs	wireless local area networks
WMANs	wireless metropolitan area networks
CFO	carrier frequency offset
ICI	inter-carrier interference
CIR	channel impulse response
SISO	single-input single-output
ML	maximum-likelihood
EM	expectation-maximization
EKF	extended Kalman filter
PSO	particle swarm optimization
FFT	fast Fourier-transform
IFFT	inverse fast Fourier-transform
ISI	inter-symbol interference
RF	radio frequency
P/S	parallel-to-serial
S/P	serial-to-parallel
IEKF	iterative extended Kalman filter
MSE	mean square error
GA	genetic algorithm
SNR	signal-to-noise-ratio
PDP	power delay profile
CRB	Cramer Rao bound

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